

BENDING PROPERTIES OF STEEL SHEET PILES PARTIALLY COVERED BY REINFORCED CONCRETE

By Osamu KIYOMIYA*, Hiroshi YOKOTA** and Takatoshi NOGUCHI***

A steel sheet pile in marine environments may have been damaged greatly by corrosion. Reinforced concrete covering is an effective repair technique for such damaged steel sheet piles. The repaired part of the sheet piles can be designed as a composite structure with reinforced concrete and the steel. Its design method and structural details have to be made clear. Loading tests on eight test specimens have been undertaken to investigate their mechanical properties and to verify the design formulae. Through the loading tests, ultimate strength, crack development, and so on depended on the arrangement of shear connectors and concrete cover length.

Keywords : composite beam, loading test, steel sheet pile, repair work

1. INTRODUCTION

Steel sheet piles have been used rather frequently for port and harbour facilities such as piers and seawalls. Corrosion is feared in steel which is in contact with sea water. Severe corrosion is limited in the zone between high and low water levels. Anti-corrosion methods and repair methods are required to be established. As a repair method for damaged steel sheet piles, reinforced concrete covering technique has been frequently used in port and harbour facilities. The concrete covering will be applied to the part where its sectional stiffness is remarkably decreased. At the covered part, reinforced concrete and the steel sheet pile are mechanically combined by studs. The method on design and installation is summarized in the Manual¹⁾. However, sufficient discussion on strength and durability of the concrete covering method has not been made, and many technical problems are remaining. In particular, how to compose the two materials and how to estimate the strength of the composite pile are not made clear. In the present paper, these problems are examined by loading tests and the applicability of the design formulae in the Manual is discussed.

2. BACKGROUND OF INVESTIGATION

(1) Corrosion of steel sheet pile

Steel sheet piles are installed in front of a pier as illustrated in Fig. 1. Steel sheet piles are located between an upper slab and sea mud. According to corrosion investigation^{2),3)}, corrosion amount along steel sheet piles which have been used for 14 years is obtained in Fig. 2.

* Member of JSCE, Dr. Eng., Chief, Structural Mechanics Laboratory, Port and Harbour Research Institute, Ministry of Transport (Nagase 3 chome 1-1, Yokosuka-shi, Kanagawa)

** Member of JSCE, M. Eng., Deputy head of Yokohama Investigation and Design Office, Ministry of Transport

*** Member of JSCE, Member of Structural Mechanics Laboratory, Port and Harbour Research Institute, Ministry of Transport

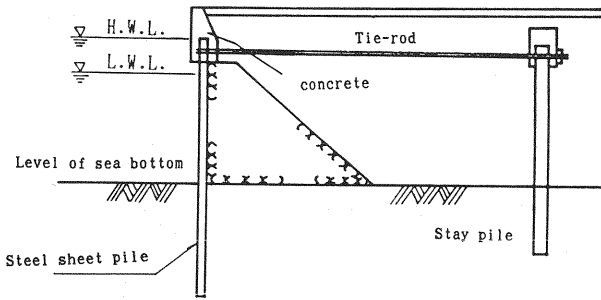


Fig. 1 Example of Steel Sheet Pile in Pier.

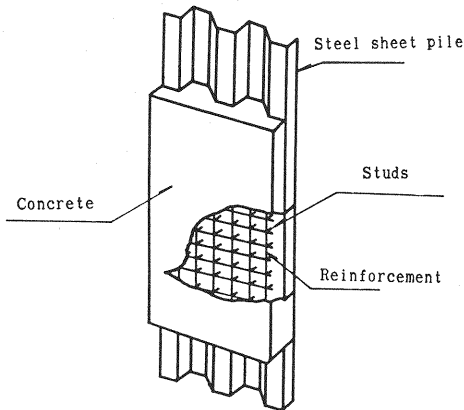


Fig. 3 Outline of the Reinforced Concrete Covering Method.

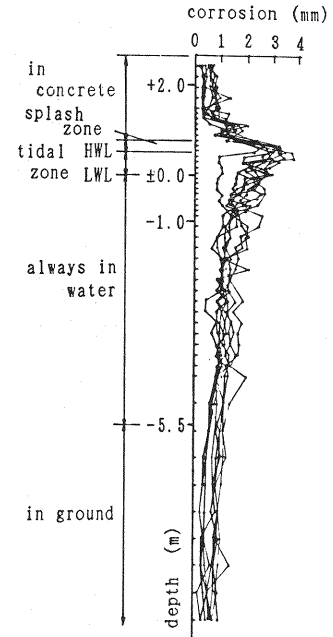


Fig. 2 Corrosion Amount of Sheet Piles.

(2) Outline of repair method

The purpose of repair work is to restore the lost strength of a steel sheet pile. When stress calculated against design external forces exceeds an allowable stress, or when calculated stress is feared to exceed an allowable stress near future, repair work should be considered. Although various methods for repair have been proposed⁴⁾, the reinforced concrete covering method⁵⁾ is frequently employed. The outline of this method is shown in Fig. 3. Rust and sticking organisms on a steel sheet pile are removed by surface preparation. Studs of 12 to 16 mm in diameter are welded by a stud gun to the steel sheet pile followed by arranging additional reinforcements in front of steel sheet piles. Concrete is cast into the form. The thickness of the covering concrete is usually about 250 mm and concrete cover to embedded steel bars is more than 70 mm. The covering range is usually from the lower end of an upper slab through about the part at L. W. L. -2.0 m. After the repair, both steel sheet piles and the reinforced concrete resist external forces. In other words, the part where repair work has been done, can be considered as a composite member.

3. CALCULATION METHOD ON COMPOSITE STEEL SHEET PILE

(1) Strength as composite steel sheet pile

Induced stresses due to flexural moment can be calculated with the following method.

a) Calculation of neutral axis depth

On the assumption that strain is proportional to the distance from the neutral axis, the following formula is derived, which is schematically shown in Fig. 4. Here, the tensile strength of concrete is not taken into consideration and a steel sheet pile and the reinforced concrete are assumed to be completely composed.

$$E_s \epsilon(x-d_t)A_s + E_s \epsilon(x-d_c)A'_s + E_s \int_{x-H_s}^x b_{sy} \epsilon(y) dy + E_c \int_0^{x-t} b_c \epsilon(y) dy = 0 \quad (1)$$

where, E_s : modulus of elasticity of steel

E_c : modulus of elasticity of concrete

x : neutral axis depth

d_t : distance from the compression edge to tensile reinforcement

d_c : distance from the compression edge to compressive reinforcement

A_s : cross sectional area of tensile reinforcement

A'_s : cross sectional area of compressive reinforcement

b_{sy} : effective width of steel sheet pile

b_c : width of concrete

ϵ : strain in general

t : flange thickness of steel sheet pile

y : distance from the neutral axis

H_s : height of one pair of steel sheet piles

From the distribution of strains, the following relationship is obtained.

$$\frac{\epsilon(x-d_t)}{x-d_t} = \frac{\epsilon(x-d_c)}{x-d_c} = \frac{\epsilon(y)}{y} \quad (2)$$

$$\frac{E_s}{E_c} = n \quad (3)$$

The effective width of concrete in compression is obtained as follows :

$$b_c(y) = b_2 - \frac{b_2 - b_1}{H_s} (H_s - x + y) = \frac{1}{H_s} [b_1 H_s + (b_2 - b_1)x - (b_2 - b_1)y] \quad (4)$$

where, b_1 : flange width of steel sheet pile in compression side

b_2 : flange width of steel sheet pile in tension side

B : width per one pair of steel sheet piles ($= b_1 + b_2$)

Now, substitute Eq. (1) into Eq. (4),

$$n[(x-d_t)A_s + (x-d_c)A'_s + A_{sy}(x-g)] + \frac{1}{H_s} [b_1 H_s + (b_2 - b_1)x] \frac{(x-t)^2}{2} - \frac{1}{H_s} (b_2 - b_1) \frac{(x-t)^3}{3} = 0 \quad (5)$$

where, A_{sy} : cross sectional area of steel sheet pile

g : neutral axis depth of steel sheet piles themselves

Here, t is neglected because it is considerably smaller than x .

$$\frac{1}{6} \frac{b_2 - b_1}{H_s} x^3 + \frac{b_1}{2} x^2 + n(A_s + A'_s + A_{sy})x - n(A_s d_t + A'_s d_c + A_{sy} g) = 0 \quad (6)$$

Position of neutral axis can be calculated by solving above formula.

b) Calculation of bending stiffness

Assuming x_0 as the solution obtained from Eq. (6), bending stiffness (S) of composite steel sheet pile is given by Eq. (7). Here, t is neglected again.

$$S = E_s[(x_0 - d_t)^2 A_s + (x_0 - d_c)^2 A'_s + I_{sy}] + E_c \left(\frac{b_2 - b_1}{12 H_s} x_0^4 + \frac{b_1}{3} x_0^3 \right) \quad (7)$$

where, I_{sy} : moment of inertia of steel sheet pile, taking the joint efficiency^(6,7) into consideration

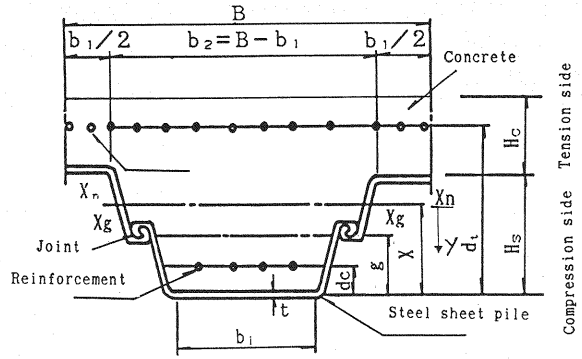


Fig. 4 Cross Section of a Covered Steel Sheet Pile.

c) Calculation of stress

Stresses in respective parts where flexural moment is increased after the repair, are expressed by the following formulae.

$$\sigma_s = E_s \frac{M}{S} (d_t - x_0) \dots \dots \dots (8)$$

$$\sigma'_s = E_s \frac{M}{S} (x_0 - d_c) \dots \dots \dots (9)$$

$$\sigma_{sy} = E_s \frac{M}{S} (H_s - x_0) + \frac{M_0}{Z_{sy}} \dots \dots \dots (10)$$

$$\sigma'_{sy} = E_s \frac{M}{S} x_0 + \frac{M_0}{Z'_{sy}} \dots \dots \dots (11)$$

$$\sigma'_c = E_c \frac{M}{S} (x_0 - t) = E_c \frac{M}{S} x_0 \dots \dots \dots (12)$$

where, M_0 : flexural moment at the repair

M : increase in flexural moment after the repair

σ_s : tensile stress of reinforcement

σ'_s : compressive stress of reinforcement

σ_{sy} : tensile stress of steel sheet pile

σ'_{sy} : compressive stress of steel sheet pile

σ'_c : stress at the compression edge of concrete

Z_{sy} : sectional modulus of steel sheet pile in tension side

Z'_{sy} : sectional modulus of steel sheet pile in compression side

In addition, mechanical and chemical characteristics of steel sheet piles which were exposed to sea water for long time do not change on the basis of investigation⁹⁾.

(2) Number of studs⁹⁾

Composition of reinforced concrete and steel sheet piles is accomplished through studs, which are arranged along the steel sheet pile with appropriate intervals as shown in Fig.5. The necessitated number of studs is calculated by the following formula¹⁾.

$$Q_t = \frac{M}{n_t y_t^2 + n_c y_c^2} y_t \leq Q_a \dots \dots \dots (13)$$

$$Q_c = \frac{M}{n_t y_t^2 + n_c y_c^2} y_c \leq Q_a \dots \dots \dots (14)$$

where, M : increase in flexural moment

Q_a : allowable shearing force

Q_t, Q_c : shearing forces act on a stud in tension side and in compression side respectively

n_t, n_c : number of studs in tension side and in compression side respectively

y_t, y_c : distance from the neutral axis to lower ends of studs in tension side and in compression side respectively

Both calculated shear forces should be less than the allowable shear force. Pull-out forces of studs from concrete are also confirmed to be smaller than the allowable force, which will be described in 5. (3).

4. LOADING TEST

(1) Test specimen

Flexural loading tests on 8 test beam specimens have been undertaken. The outline of the specimens is summarized in Table 1. Their overall length and width are identical of 5.0 m and 1.6 m respectively. Fig. 6

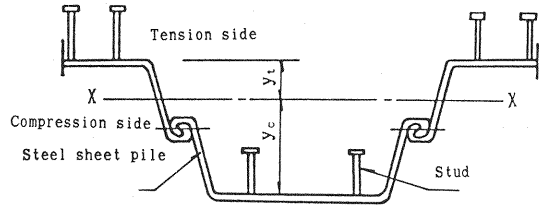


Fig.5 Arrangement of Studs.

Table 1 List of test specimen.

No.	Kind	Initial stress	Kinds of concrete
No. 1	Reinforced concrete covering method Number of studs : 40	Not applied	Ordinary Portland cement
No. 2	Reinforced concrete covering method Number of studs : 40	1800 kgf/cm ²	Rapid hardening cement
No. 3	Reinforced concrete covering method Number of studs : 40	3000 kgf/cm ²	Rapid hardening cement
No. 4	Reinforced concrete covering method Number of studs : 15	Not applied	Ordinary Portland cement
No. 5	Reinforced concrete covering method Stud connector with head: 36 J type stud connector : 36	Not applied	Ordinary Portland cement
No. 6	Reinforced concrete covering method Headed studs : 72 Stirrups : 45	Not applied	Ordinary Portland cement
No. 7	Steel sheet pile only	Not applied	
No. 8	Reinforced concrete only	Not applied	Rapid hardening cement

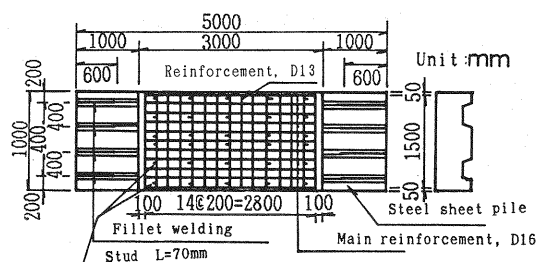


Fig. 6 Structure of Test Beam.

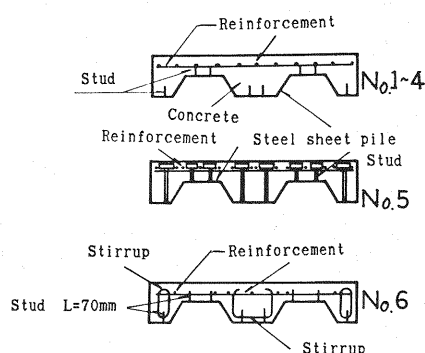


Fig. 8 Arrangement of Shear Connectors.

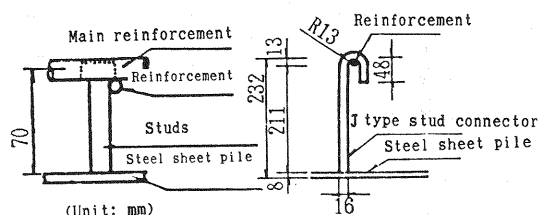


Fig. 7 Structure of Shear Connectors.

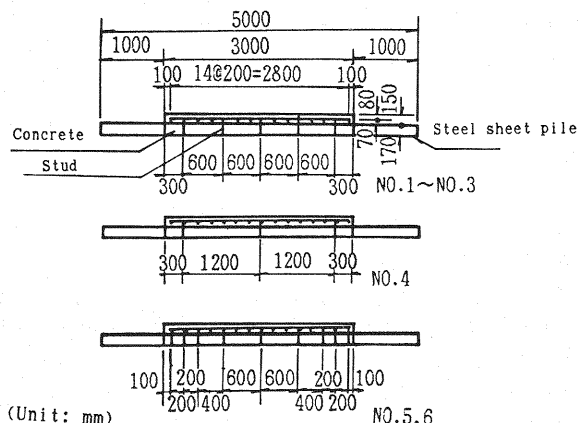


Fig. 9 Arrangement of Studs in Axial Direction.

shows the details of No. 1 beam. Four steel sheet piles of SP-IA, Grade SY 30 are assembled to fabricate one beam. Central part of 3.0 m is covered by reinforced concrete. Deformed reinforcing bars of 16 mm in diameter and Grade SD-30 A are arranged longitudinally at intervals of 150 mm. In addition, those of 13 mm in diameter and Grade SD-30 A are arranged transversely at intervals of 150 mm. Shear connectors of headed studs and stirrups are installed for composing the reinforced concrete and the steel sheet piles. In Nos. 1 through 4 beams, headed studs of 16 mm in diameter and 75 mm in length are welded to the steel

Table 2 Mix Proportion of Concrete.

Ordinary concrete (kgf/m ³)						
Cement	Water	Fine aggre- gate	Coarse aggre- gate	Coarse aggre- gate	Mixing agent	Mixing agent
278	165	838	506	514	2.87	-
Water/cement ratio: 57.8%, Maximum size of aggregate: 25mm						
Fine aggregate ratio: 45.7%, Slump: 15cm, Air: 4%						
Rapid hardening concrete (kgf/m ³)						
Cement	Water	Fine aggre- gate	Coarse aggre- gate	Coarse aggre- gate	Mixing agent	Mixing agent
300	168	820	506	514	3.00	-
Water/cement ratio: 56.0%, Maximum size of aggregate: 25mm						
Fine aggregate ratio: 45.1%, Slump: 15cm, Air: 4%						

Table 3 Strength of Concrete.

No.	Compressive strength (kgf/cm ²)	Tensile strength (kgf/cm ²)	Young's modulus (kgf/cm ²)	Poisson's ratio
No.1	215	21.2	2.06×10^5	0.16
No.2	224	22.8	2.40×10^5	0.18
No.3	311	22.4	2.85×10^5	0.20
No.4	215	19.0	2.26×10^5	0.17
Nos.5,6	308	18.0	2.31×10^5	0.21
No.8	233	22.1	2.69×10^5	0.23

*) No.2 and No.3 are rapid hardening cement

Table 4 Strength of Steel.

Material	Grade	Yield strength (kgf/cm ²)	Tensile strength (kgf/cm ²)	Elastic modulus (kgf/cm ²)	Elongation (%)
Steel sheet	JIS A				
pile	5528	4600	5900	2.03×10^6	21.5
SP - 1A	SY30				
Reinforce- ment	JIS G				
D13	3112	3666	5390	-	24.2
	SD30				
Reinforce- ment	JIS G				
D16	3112	3800	5500	-	28.0
	SD30				
Stud	JIS B				
	1197	-	4280	-	26.0
M16	SWCH				

sheet piles. In No. 5 beam, J-shaped reinforcement approximately 230 mm in length, and in No. 6 beam, stirrups in 13 mm diameter are used. Fig. 7 shows the details of the shear connectors. The arrangement of the shear connectors are shown in Figs. 8 and 9. The studs are arranged on the flange of the steel sheet piles in 2 lines at intervals of 600 mm for Nos. 1 through 3 beam and in 1 line at intervals of 1 200 mm for No. 4 beam. The number of studs is decided to resist shear forces by Eqs. (13) and (14). In test specimens of No. 5 and No. 6, shear connectors are arranged densely at the end of reinforced concrete.

In Nos. 2 and 3 beams, initial stresses of 1 800 kgf/cm² and 3 000 kgf/cm² are introduced respectively to the steel sheet pile before concrete casting. The initial stress simulates actual conditions; that is, fairly large stress is already induced in steel sheet piles at their thin parts due to earth and water pressures before repair work. The beams are strengthened by steel plates at the loading points and the supports to prevent from widening and twisting. The beams of steel sheet piles only (No. 7) and reinforced concrete only (No. 8) are also fabricated to confirm the effectiveness of the concrete covering.

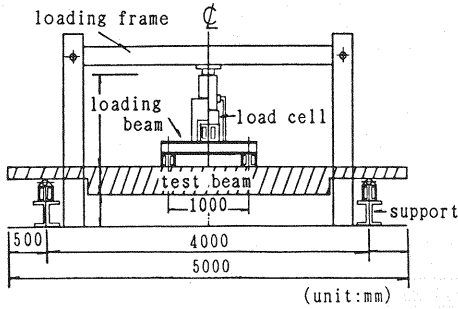


Fig. 10 Test Set-up for the Beams.

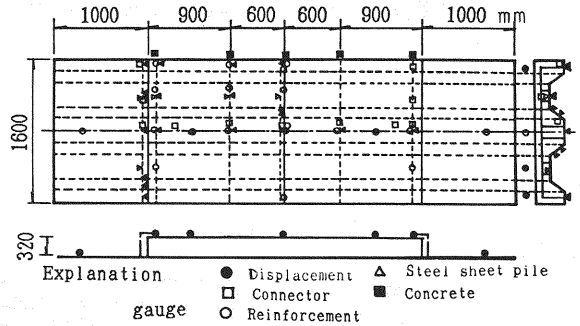


Fig. 11 Positions of Measurement.

(2) Used materials

Cements used for the concrete are either ordinary Portland cement or rapid hardening cement. Mix proportions of the concrete are presented in Table 2. Design strength of the concrete is 240 kgf/cm² and its slump is about 150 mm. Table 3 presents the compressive strength of the concrete at the loading tests. The mechanical characteristics of the steel are summarized in Table 4.

(3) Loading

Fig. 10 shows the test set-up. Load is applied from the steel sheet pile side symmetrically at two points. The distances between the supports and between the loading points are 4.0 m and 1.0 m respectively. A manually operated hydraulic jack is used for applying the load which is increased monotonously. Loading is quitted when distinct failure appears.

(4) Instrumentation

Measurements are made during the test as follows : applied loads by a load cell ; deflection of the beam by displacement transducers ; slip and separation by displacement transducers ; strains of the steel sheet pile, reinforcing bars, and concrete by strain gauges ; width of crack by contact-type gauges ; propagation of cracks by visual inspection.

The arrangement of measuring instruments slightly differs among the test beams. Fig. 11, for example, shows the arrangement in No. 1 beam.

5. RESULTS OF TEST AND DISCUSSION

(1) Development of cracks and mode of failure

Formation of cracks in Nos. 1, 5, and 6 beams are shown in Figs. 12, 13, and 14 respectively. In No. 1 beam, cracks were initiated at the central parts when the load was 4 tf and then numbers of cracks increased. When the load reached 16 tf, cracks occurred horizontally at the end of the concrete. These cracks were caused by shear and tensile collapse of concrete around studs. When the load reached 32 tf,

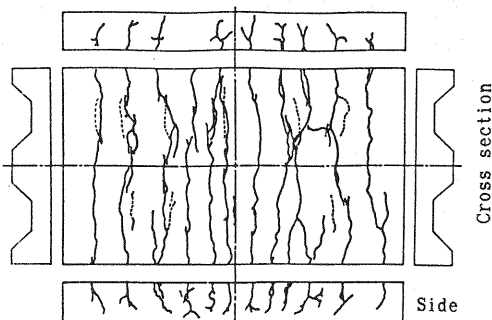


Fig. 12 Crack Formation in No. 1 Beam.

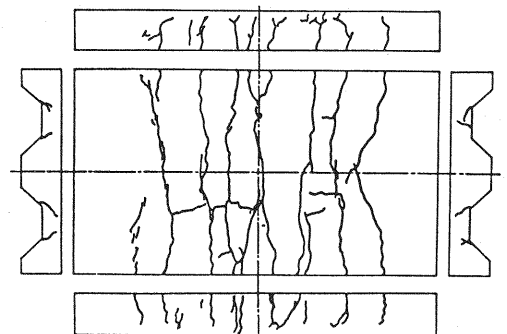


Fig. 13 Crack Formation in No. 5 Beam.

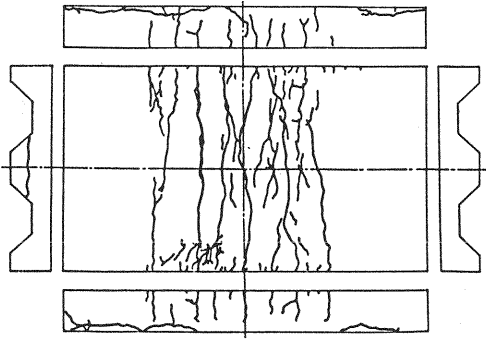


Fig. 14 Crack Formation in No. 6 Beam.

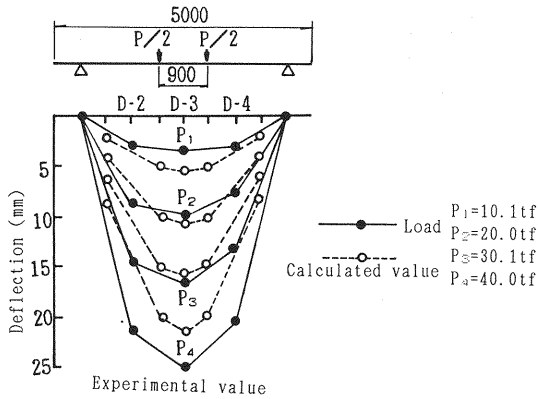


Fig. 16 Distribution of Deflection (No. 4 beam).

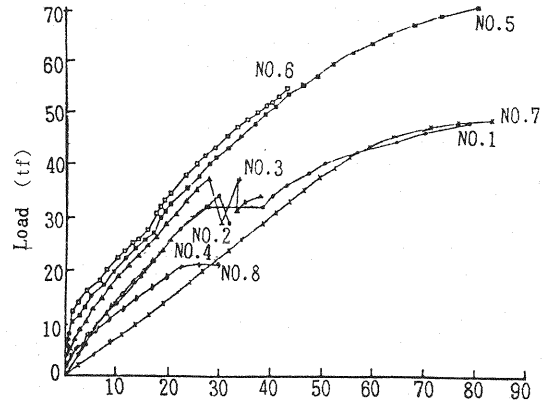


Fig. 15 Relationship between Load and Midspan Deflection.

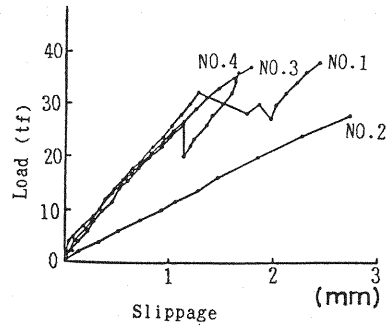


Fig. 17 Relative Displacement at the End of Reinforced Concrete.

concrete was crushed in conical shape around studs, and the steel sheet pile and the reinforced concrete separated at its end. Failure of the test beam subsequently progressed and buckling at the compression edge of the steel sheet pile was finally observed.

The process of failure of Nos. 2 through 4 beams showed almost similar to that of No. 1 beam. In No. 5 beam, initial cracks occurred at the load of 9.2 tf followed by developing flexural cracks. Finally, crushing of concrete between the loading points was observed. However, the failure at the end of the concrete, like of No. 1 beam, was not observed. The ultimate load of No. 5 beam was the largest among the test beams. In No. 6 beam, flexural cracks developed like the other test beams, but in final stage, shear failure of concrete was observed near the stirrups.

After the loading tests, tensile fracture of the embedded steel was investigated, which made clear that the studs and the reinforcing bars did not collapse.

(2) Relationship between load and displacement

The relationship between load and deflection at the midspan of the test beams is shown in Fig. 15. The calculated maximum flexural moment of the test beams by Eq. (7) is 12.2 tf·m, which is 31.3 tf in terms of the load. Here, the allowable stress of the steel is 2700 kgf/cm², which is the value of 1.5 times the ordinary allowable one. It can be said that Nos. 1 through 6 beams had higher yield strengths than the designed value anyhow. Nos. 1 through 4 beams, however, did not have sufficient surplus strengths and rigidities because of destruction caused by pull-out shear of concrete at the end of reinforced concrete. Therefore, their mechanical properties were not good. Long studs or stirrups should be necessary. Initial stiffnesses of the test beams where initial stress was introduced showed no remarkable difference compared to that without initial stress (No. 1 beam), but their ultimate loads were slightly smaller than that of No. 1 beam.

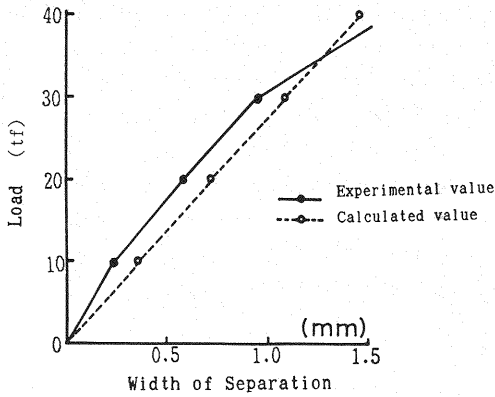


Fig. 18 Separation of the Steel Sheet Pile and Concrete.

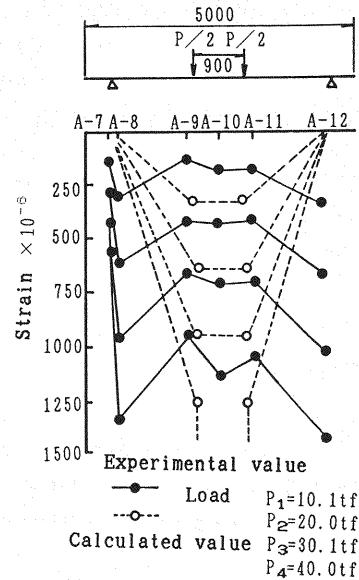


Fig. 19 Distribution of Strain.

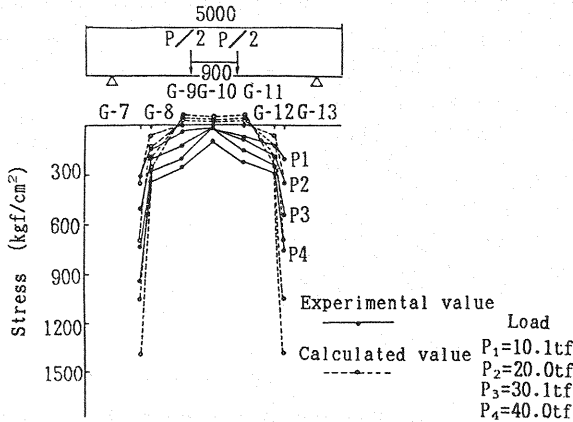


Fig. 20 Stress of Studs.

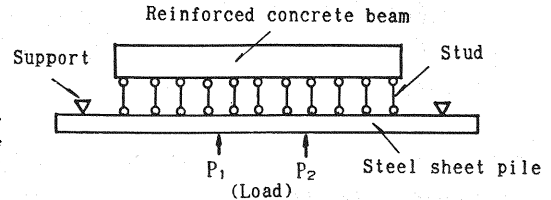


Fig. 21 Calculation Model for Pull-out Forces of Studs.

The distributions of deflection of No. 4 beam at the loads of 10, 20, 30, and 40 tf are shown in Fig. 16. While the load was small, the distribution of the deflection bent at D-2 and D-3 in the figure where the sectional modulus changed. With increase in the load, the concrete covered part showed large deflection because of the occurrence of cracks. The calculated values of deflection obtained as a complete composite beam are also shown in the figure. In this calculation, the joint efficiency^(6),7) of U-type sheet piles is determined to be 0.83. This value is obtained from the loading test on No. 7 beam. The experimental value and the calculated value showed fairly good agreement until the steel yielded.

Fig. 17 shows relative displacement (slip) between the steel sheet piles and the concrete at its end. The relative displacement was about 1 mm at the load of 30 tf. Fig. 18 shows the width of separation at the same position. Separation began when the load was small, and its width reached as large as 1.0 mm at the load of 30 tf. The slip is related to the degree of composition, and the separation is both the degree of composition and the durability of materials.

(3) Distribution of strain

Fig. 19 shows the longitudinal strain distribution of the steel sheet piles at its compression edge of No. 4 beam. Remarkably large strains occurred near the studs at the end of the concrete. Axial stress of the studs in No. 4 beam is shown in Fig. 20. These values are obtained by a pair of strain gauges attached to studs. Axial stress was dominant in the studs. As shown in this figure, large pull-out forces occurred at the end of the concrete.

Thus, the strength and the durability of the composite beam are greatly affected by the separation at the end or the pull-out of the studs from the concrete. To take the results into consideration for designs, a

calculation model shown in Fig. 21 is proposed here which can estimate the separation and the pull-out force. In the model, the concrete and the steel sheet pile are replaced to beams and the studs are replaced to springs. The separation should be calculated taking account of elongation of studs and bond behaviours of surrounding concrete. Here, the separation is defined as the elongation of studs themselves, which will provide the conservative solution.

Figs. 18 and 20 show the comparison between the experimental results and the calculated ones on the separation and the pull-out force. From the comparison, the experimental results and the calculated results showed good agreement. Therefore, the simple calculation model in Fig. 21 can apply to estimate the separation and the pull-out forces of studs, while cracking, the correlation of pull-out and shear forces, and so on occur in actual beams.

6. CONCLUSIONS

The following main conclusions are obtained from the present research.

(1) To compose reinforced concrete partially on steel sheet piles, it is necessary to provide sufficient reinforcement at the end of the reinforced concrete coverage. If shear connectors are not fixed tightly on tensile reinforcement, concrete around the shear connectors is collapsed and the stiffness of the composite beam shows rapid deterioration by pull-out tensile forces at the end of the concrete coverage. When long studs or stirrups are used, such phenomena are not observed. Therefore, strength and rigidity of the test specimens are not against expectation, hence composing of steel sheet piles and reinforced concrete is insured.

(2) As considerable stress concentration on studs was observed at the end of reinforced concrete coverage, it is necessary to give consideration on both shear and pull-out of studs there. It is also necessary to arrange more studs than at the other parts, or to use longer shear connectors.

(3) The slip of steel sheet piles and reinforced concrete at its end is not so much but separation is found at the relatively small load stage. Careful attention is required because there is a danger of corrosion caused by penetration of sea water. The values of separation and pull-out forces of studs are approximately calculated by the simple calculation model proposed in this paper.

(4) When initial stress is introduced into steel sheet piles before composing, the yield strength and initial stiffness are almost similar to those without initial stress until the yield of tension reinforcement.

(5) By the calculation formula of bending yield strength of composite beams shown in this paper, calculated yield strength of the test specimen was larger than the experimental values. However, as described in Conclusion (1), it is impossible to maintain sufficient toughness or deformation capacity without careful attention on structural details of shear connectors, and so on.

(6) For the calculation of bending stiffness of composite beams, it is necessary to take the joint efficiency (rate of stiffness decrease caused by slipping at joint) of U-type steel sheet piles into consideration. The joint efficiency of the test specimens in this study was about 0.8, but in practical design, the value shall be determined considering ground condition and installation condition of a structure.

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