

## EVALUATION OF EVAPORATION FLUX UNDER QUASI-UNSTEADY WIND VELOCITY

By

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## SYNOPSIS

The present paper describes a new method to calculate the hourly evaporation flux under quasi-unsteady wind velocity using a wind tunnel that can supply a set of high and low speed winds with arbitrary time intervals. Soil columns filled with Chao soil and Toyoura standard sand were used in wind tunnel evaporation experiments. The hourly averaged free-stream velocity,  $V_{w0}^{ave}$ , had the same value for all wind velocity combinations. In spite of the same  $V_{w0}^{ave}$ , the difference in the cumulative evaporation at 150 hours after the beginning of the experiment became no less than 8-12% by changing the combinations of high and low speed winds, regardless of the soil. This is attributed to the nonlinear relation between the evaporation coefficient,  $\alpha_v$ , and the free-stream velocity,  $V_{w0}$ . Findings show that the hourly evaporation flux calculated using two different  $\alpha_v$  values for high and low wind velocities is more accurate than that calculated using  $\alpha_v$  for  $V_{w0}^{ave}$ .

## INTRODUCTION

The problem of evaporation is closely related to the preservation of water resources for drinking and irrigation water, soil hazards due to salt, heat islands, global warming, etc.

A lysimeter and an evaporation pan (a soil tank) are used to measure evaporation or evapotranspiration. The evaporation flux is obtained by calculating the decrease in the weight of the soil tank associated with evaporation over

the time interval of the measurement. Saito et al. (1) found that a lysimeter tends to overestimate evapotranspiration for several days after rainfall, although there was no deterioration of the measuring system. Since a rule or a balance is used for the measurement of evaporation with an evaporation pan, automatic and sequential collection of data are difficult in the field. Much work is, therefore, necessary for long-term observations.

The eddy correlation method is also a widely used technique. In this method, evaporation is calculated from a direct measurement of turbulent transport and is useful to the diagnosis of the transport of the sensible heat, latent heat and CO<sub>2</sub> between the land (or sea) and the atmosphere (Tamagawa (2), Narimatsu et al. (3), Machimura (4), Iwata et al. (5)). This method requires, however, much maintenance and human work to carry out regular calibrations and to get adjustments of the hygrometer and the anemometer. Moreover, it is necessary to examine whether the vapor flux, calculated at a measurement point, fully represents evaporation from the ground or water surface under the measurement point.

On the other hand, the energy balance method is a common indirect method (Kondo (6), Kimura et al. (7)). Of course in this method the accuracy of the evaporation depends on the measurement accuracy of short- and long-wave radiation, ground heat and the sensible heat due to wind.

The time variation of the wind velocity also makes the evaluation of the evaporation difficult. Generally evaporation may be evaluated over time scales of hours or days in the field. Therefore, we conducted an evaporation experiment by means of a soil column, filled with Toyoura standard sand (T-soil), under a quasi-unsteady wind velocity by switching high and low speed winds at intervals of  $\Delta t$  (minutes) (Kadono et al. (8)). As a result, the difference in the hourly evaporation flux (HEF) reached a maximum of 12% compared with our previous wind tunnel evaporation experiments, although the hourly averaged wind velocity had the same value for all combinations of high and low speed winds. The soil surface temperature and the wind velocity during the transient period between the high and low speed winds were measured for Chao soil (C-soil) and T-soil in the present wind tunnel evaporation experiments.

This paper describes the characteristics of vapor transfer from the soil surface to the air during the transient period and proposes a new evaporation model to calculate the HEF precisely.

## CALCULATION OF EVAPORATION FLUX

### *Properties of evaporation model*

The bulk type equation for water vapor is widely applied to evaluate evaporation flux from the soil surface (Kondo (9)). The evaporation flux,  $E_v$ , for the present wind tunnel evaporation experiments can be computed by the following bulk type equation:

$$E_v = \rho C_E (q_s - q_{a0}) V_{w0} \quad (1)$$

where,  $E_v$  = mass evaporation flux (kg/m<sup>2</sup>/s);  $\rho$  = air density (kg/m<sup>3</sup>);  $C_E$  = bulk coefficient of evaporation (-);  $q_s$  = specific humidity on the soil surface (kg/kg);  $V_{w0}$  = free-stream velocity (m/s) (= wind velocity in the free-stream region formed in the outer region of the logarithmic velocity profile, see Fig.3); and  $q_{a0}$  = specific humidity of the air in the free-stream region (kg/kg). It is seen that  $E_v$  varies linearly with  $V_{w0}$  when  $C_E$  and  $(q_s - q_{a0})$  are constant.

$E_v$  (henceforth, evaporation flux) is calculated by Eq. 2 instead of Eq. 1 in this paper.

$$E_v = \alpha_v D_{atm} (\rho_{vsurf} - \rho_{vair0}) \quad (2)$$

in which  $\alpha_v$  = evaporation coefficient (1/m);  $D_{atm}$  = diffusion coefficient of vapor in air ( $m^2/s$ );  $\rho_{vsurf}$  = vapor density on the soil surface ( $kg/m^3$ ); and  $\rho_{vair0}$  = vapor density of the air in the free-stream region ( $kg/m^3$ ).  $\rho_{vsurf}$  is assumed to be the saturated vapor density and is given by a function of the soil surface temperature,  $T_{surf}$ , i.e.  $\rho_{vsurf}(T_{surf})$ .  $\alpha_v$  is expressed in terms of  $V_{w0}$  (Kadono et al. (8)). The vapor-density difference,  $(\rho_{vsurf} - \rho_{vair0})$ , and  $\alpha_v$  yield the driving force of the evaporation and the evaporativity due to the movement of air (convection) on the soil surface, respectively.

#### Hourly evaporation flux (HEF)

Eq. 3 is a conventional model adopted to calculate the HEF,  $E_{vh1}$  ( $kg/m^2/hr$ ),

$$E_{vh1} = 3600(E_v)_{60} \quad (3)$$

The evaporation flux,  $(E_v)_{60}$  ( $kg/m^2/s$ ), is calculated by the following expression of Eq. 4

$$(E_v)_{60} = \alpha_v (V_{w0}^{ave}) D_{atm} \{ \rho_{vsurf}(T_{surf}^{ave}) - \rho_{vair0} \} \quad (4)$$

The value of  $\alpha_v$  is determined from the hourly averaged free-stream velocity,  $V_{w0}^{ave} (= (V_{w0}^{high} + V_{w0}^{low})/2)$ , where  $V_{w0}^{high}$  and  $V_{w0}^{low}$  are the  $V_{w0}$  of high and low speed winds, respectively (see Figs. 2 and 6).  $\rho_{vsurf}$  is calculated from the averaged soil surface temperature,  $T_{surf}^{ave} (= (T_{surf}^{high} + T_{surf}^{low})/2)$ , where  $T_{surf}^{high}$  and  $T_{surf}^{low}$  are the values of  $T_{surf}$  in the equilibrium state for  $V_{w0}^{high}$  and  $V_{w0}^{low}$ , respectively (see Fig. 8).

A new model for calculating the HEF ( $E_{vh2}$ ) is introduced in this section.  $E_{vh2}$  takes into account the nonlinear relation between  $\alpha_v$  and  $V_{w0}$ , which will be shown in the section “Evaporation coefficient and evaporation flux”.  $E_{vh2}$  can be obtained by summing the cumulative evaporation for all time intervals  $\Delta t$  (minutes) over one hour. That is

$$E_{vh2} = 60 \Delta t \sum_{i=1}^n (E_{vi})_{\Delta t} \quad (5)$$

in which  $n$  represents the switching number of the wind velocity given by  $n = 60/\Delta t$ .

The evaporation flux,  $(E_v)_{\Delta t}$  ( $kg/m^2/s$ ), is denoted by  $(E_v)_{\Delta t}^{high}$  and  $(E_v)_{\Delta t}^{low}$ , which indicate  $(E_{vi})_{\Delta t}$  of the high and low speed winds for  $\Delta t$ , respectively.

$$(E_v)_{\Delta t}^{high} = \alpha_v (V_{w0}^{high}) D_{atm} \{ \rho_{vsurf}(T_{surf}^{high}) - \rho_{vair0} \} \quad \text{for the high speed wind} \quad (6)$$

$$(E_v)_{\Delta t}^{low} = \alpha_v (V_{w0}^{low}) D_{atm} \{ \rho_{vsurf}(T_{surf}^{low}) - \rho_{vair0} \} \quad \text{for the low speed wind} \quad (6)'$$

The value of  $\alpha_v$  is determined individually from  $V_{w0}^{high}$  or  $V_{w0}^{low}$ , i.e. as  $\alpha_v(V_{w0}^{high})$  and  $\alpha_v(V_{w0}^{low})$ .  $\rho_{vsurf}$  is calculated from  $T_{surf}^{high}$  or  $T_{surf}^{low}$ , respectively.

## WIND TUNNEL EVAPORATION EXPERIMENTS

Wind tunnel evaporation experiments were carried out by using a wind tunnel in the National Research Institute

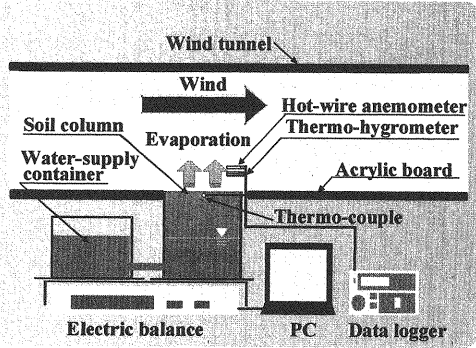


Fig. 1 Experimental equipment

Table 1 Physical properties of soils used in the experiment

Physical properties	Chao soil (C-soil)	Toyoura standard sand (T-soil)
Saturated hydraulic conductivity $k_{sat}$	$9.42 \times 10^{-5}$ (m/s)	$2.04 \times 10^{-2}$ (m/s)
The average particle diameter $D_{50}$	0.017 (mm)	0.183 (mm)
Porosity $\varepsilon$	0.40	0.39
Soil classification	Silty clay loam	Sandy soil

for Disaster Prevention. The wind velocity and  $\Delta t$  were automatically controlled from the operator control panel. The present experiment was divided into two wind conditions. The first was a steady evaporation experiment carried out to obtain HEF and the  $\alpha_v - V_{w0}$  relation under a single wind velocity. The second was a quasi-unsteady evaporation experiment to obtain HEF under the repetition of high and low speed winds.

#### Experimental equipment

The wind tunnel evaporation experiment consisted of a wind tunnel (width: 1m, height: 1m, and length: 3m), a soil column (inner diameter: 0.075m and height: 0.08m), an electric balance (minimum reading: 0.01g), a thermo-hygrometer, a hot-wire anemometer and a thermo-couple (see Fig. 1). The bottom of the wind tunnel was covered with acrylic boards.

Table 1 shows the physical properties of C-soil and T-soil used in the experiment, respectively. The C-soil is silty clay loam and its average particle diameter is about one tenth of that of T-soil.

#### Experimental procedure and conditions

The T-soil and C-soil were packed in a soil column with a dry density of  $1600\text{kg/m}^3$  and  $1500\text{kg/m}^3$ , respectively, and then the soil column was filled with water using a water-supply container. The soil column was adjusted so that the soil surface became level with the bottom of the wind tunnel. The air temperature and relative humidity were measured from the soil surface up to a height of 0.4m at intervals of 0.005 to 0.05m and were automatically stored in a computer.  $T_{surf}^{low}$  was measured with a thermo-couple inserted 5mm below the soil surface.  $E_v$  was measured by means of an electric balance placed under the soil column. The vertical profiles of the air temperature, relative humidity and wind velocity were measured by means of a thermo-hygrometer and a hot-wire anemometer, respectively.

Fig. 2 shows a schematic view of the wind conditions and wind velocities for the quasi-unsteady evaporation experiment.  $V_{w0}$ , which was chosen for the steady evaporation experiment, was less than 5.0m/s. Three different combinations of high and low speed winds were designed for the quasi-unsteady evaporation experiment as shown in Table 2.  $V_{w0}^{low}$  and  $V_{w0}^{high}$  were 0.4 and 5.0m/s for case A, 0.9 and 4.5m/s for case B, and 1.5 and 3.9m/s for case C, respectively.  $V_{w0}^{ave}$  of these three cases always had the same value (2.7m/s). The high and low speed winds were automatically changed every 15 or 30 minutes, i.e.  $\Delta t = 15$  or 30 minutes. The temperature and relative humidity of the ventilated air were controlled within  $25 \pm 1^\circ\text{C}$  and  $50 \pm 3\%$ , respectively.

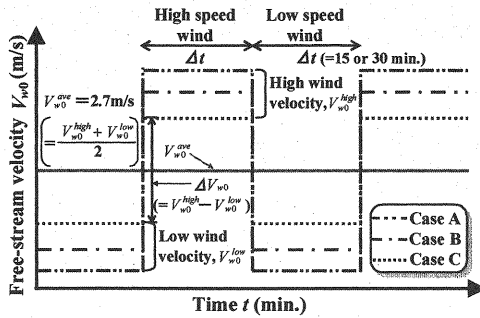


Fig. 2 Schematic view of wind conditions for quasi-unsteady evaporation experiment

Table 2 Experimental wind conditions

Soil	Chao soil and Toyoura standard sand			
Ventilated air	Temperature: $25 \pm 1^\circ\text{C}$ , Relative humidity: $50 \pm 3\%$			
Experimental cases	Free-stream velocity, $V_{w0}$			
	$V_{w0}^{\text{high}}$ (m/s)	$V_{w0}^{\text{low}}$ (m/s)	$\Delta V_{w0}$ (m/s)	$V_{w0}^{\text{ave}}$ (m/s)
Case A	5.0	0.4	4.6	2.7
Case B	4.5	0.9	3.6	2.7
Case C	3.9	1.5	2.4	2.7

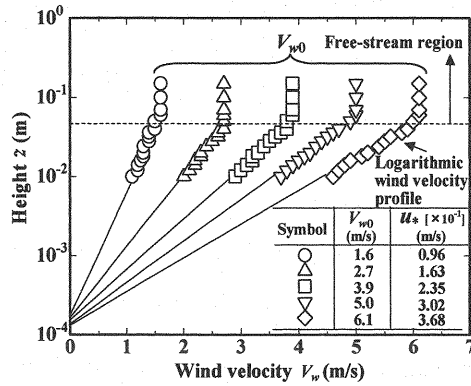


Fig. 3 Vertical profile of wind velocity in the wind tunnel

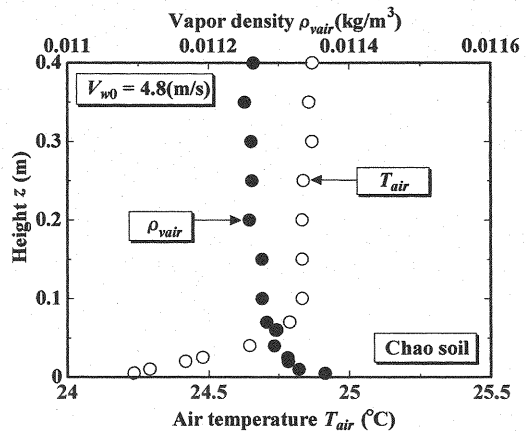


Fig. 4 Vertical profiles of air temperature,  $T_{air}$ , and vapor density,  $\rho_{vairs}$  in the wind tunnel for  $V_{w0} = 4.8\text{m/s}$  (C-soil)

## EXPERIMENTAL RESULTS

### Vertical profile of wind velocity

Fig. 3 shows the vertical profile of the wind velocity in the wind tunnel and  $V_{w0}$ . The values of the wall-friction velocity (friction velocity),  $u_*$  (m/s), and  $V_{w0}$  are also shown in Fig. 3. The logarithmic wind velocity profile expressed by Eq. 7 is valid for  $z \leq 0.05\text{m}$ .

$$\frac{V_w}{u_*} = \frac{1}{\kappa} \ln \frac{z}{z_0} \quad (7)$$

in which  $z_0$  = roughness length (m);  $z$  = vertical height from the roughness surface (m);  $V_w$  = wind velocity at  $z$  (m/s) and  $\kappa$  = Karman constant ( $\approx 0.4$ ). The average of  $z_0$  was  $1.34 \times 10^{-4}\text{m}$ .

### Vertical profiles of air temperature and vapor density in the wind tunnel

Fig. 4 shows the vertical profiles of the air temperature,  $T_{air}$ , and vapor density,  $\rho_{vairs}$  in the wind tunnel for

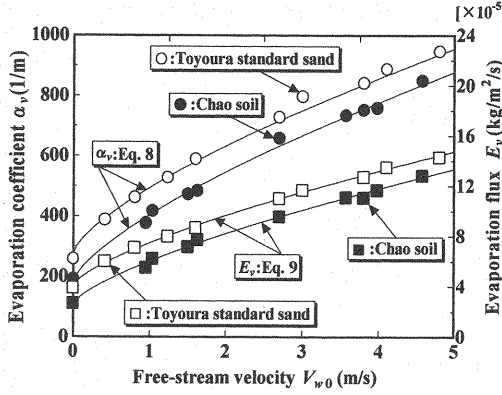


Fig. 5 Evaporation coefficient,  $\alpha_v$ , and  $V_{w0}$  relation and evaporation flux,  $E_v$ , and  $V_{w0}$  relation (C-soil and T-soil)

Table 3 Values of the coefficients  $a$ ,  $b$ ,  $c$ , and  $d$

Coefficient	Chao soil (C-soil)	Yoyoura standard sand (T-soil)
$a$ (Eq. 8)	227	221
$b$ (Eq. 8)	178	274
$c$ (Eq. 9)	$3.51 \times 10^{-5}$	$3.49 \times 10^{-5}$
$d$ (Eq. 9)	$2.51 \times 10^{-5}$	$3.99 \times 10^{-5}$

$V_{w0} = 4.8 \text{ m/s}$ .  $\rho_{vair}$  increased toward the soil surface and reached its maximum on the soil surface. On the other hand,  $T_{air}$  decreased toward the soil surface and reached its minimum on the soil surface. This profile may be attributed to the latent heat due to evaporation from the soil surface. The boundary layer thickness of  $T_{air}$  was almost the same as that of  $\rho_{vair}$ . The value of  $\rho_{vair}$  for  $z \geq 0.1 \text{ m}$  was, therefore, adopted as  $\rho_{vair0}$  in Eq. 2 and was  $1.06 \times 10^{-2} \sim 1.15 \times 10^{-2} \text{ kg/m}^3$ .

#### Evaporation coefficient and evaporation flux

Fig. 5 shows the  $\alpha_v - V_{w0}$  relation and the  $E_v - V_{w0}$  relation obtained from the steady evaporation experiment. The value of  $\alpha_v$  decreased for both C-soil and T-soil as  $V_{w0}$  became small, but the gradient,  $d\alpha_v/dV_{w0}$ , became larger as  $V_{w0}$  became smaller. The  $\alpha_v - V_{w0}$  relation for the two soils is similar to each other and  $\alpha_v$  is proportional to the 0.7th power of  $V_{w0}$  as expressed by Eq. 8, which is illustrated in Fig. 5.

$$\alpha_v = aV_{w0}^{0.7} + b \quad (8)$$

The coefficients  $a$  and  $b$  for each soil are shown in Table 3.

The  $E_v - V_{w0}$  relation has a similar distribution to the  $\alpha_v - V_{w0}$  relation, i.e.

$$E_v = cV_{w0}^{0.7} + d \quad (9)$$

Eq. 9 is shown in Fig. 5 and the coefficients  $c$  and  $d$  for each soil are shown in Table 3. It is seen that the nonlinearity of Eqs. 8 and 9 is due to appear for  $V_{w0} < 1.5 \text{ m/s}$ . As there is no significant difference in  $(\rho_{vsurf} - \rho_{vair0})$  and  $D_{atm}$  between all experimental cases, the distribution of the  $E_v - V_{w0}$  relation depends mainly on the  $\alpha_v - V_{w0}$  relation. Furthermore, it can be inferred that Eq. 1 (linearity of the  $E_v - V_{w0}$  relation) is no longer valid, if  $C_E$  and  $(q_s - q_a)$  are regarded as constants, respectively.

#### Quasi-unsteady wind velocity and evaporation

Fig. 6 shows the time variation of  $V_{w0}$  by changing from high speed wind to low speed wind and vice versa for

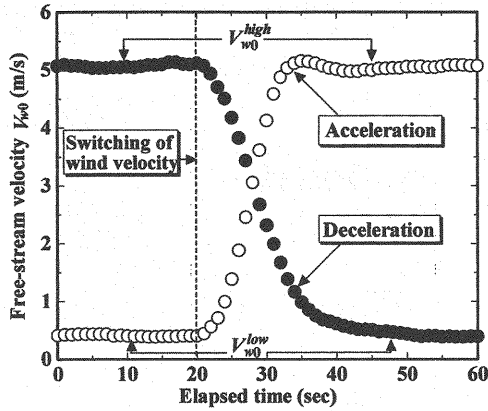


Fig. 6 Time variation of  $V_{w0}$  by changing from high speed wind to low speed wind and vice versa (case A)

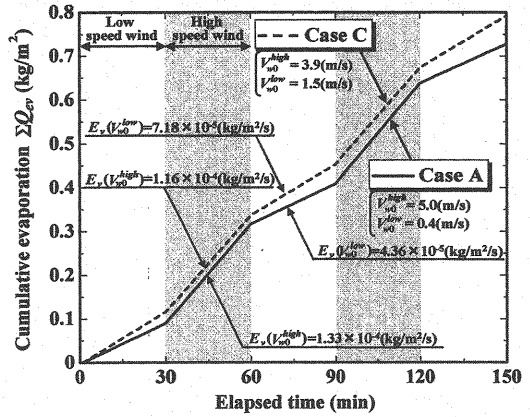


Fig. 7 Time variation of cumulative evaporation by repetition of high and low speed winds (C-soil)

case A. This transition period is termed the recovery period of  $V_{w0}$  in this paper. The recovery of  $V_{w0}$  was somewhat quicker for acceleration than for deceleration, but both recovery periods were less than 30 seconds.

Fig. 7 shows the time variation of the cumulative evaporation per unit area,  $\Sigma Q_{ev}$  ( $\text{kg/m}^2$ ), for 150 minutes from the beginning of the experiment for the C-soil.  $\Sigma Q_{ev}$  was measured for case A and case C with  $\Delta t = 30$  minutes. The time gradient of  $\Sigma Q_{ev}$  ( $= d\Sigma Q_{ev}/dt = E_v$ ) was greater for the high speed wind than for the low speed wind. The values of  $E_v$  for  $V_{w0}^{high}$  and  $V_{w0}^{low}$  are shown for case A and case C in Fig. 7. The jag of  $E_v$  from the repetition of the high and low speed winds was sharper for case A than for case C, because  $\Delta V_{w0} (= V_{w0}^{high} - V_{w0}^{low})$  for case A was greater than that for case C. The difference in  $\Sigma Q_{ev}$  between case A and case C grew with the elapsed time and finally,  $\Sigma Q_{ev}$  of case C was 1.09 times greater than that of case A at 150 minutes of the elapsed time. This difference became especially remarkable during the low speed wind, because the difference in  $E_v$  between  $V_{w0}^{low} = 1.5$  and  $0.4\text{m/s}$  (for the low speed wind),  $\Delta E_v^{low} (= 2.8 \times 10^{-5} \text{kg/m}^2/\text{s})$ , is greater than that between  $V_{w0}^{high} = 5.0$  and  $3.9\text{m/s}$  (for the high speed wind),  $\Delta E_v^{high} (= 1.7 \times 10^{-5} \text{kg/m}^2/\text{s})$ , as judged from Fig. 5, although the difference of  $V_{w0}^{low} (= 1.5 - 0.4)$  for the low speed wind and the difference of  $V_{w0}^{high} (= 5.0 - 3.9)$  for the high speed wind were the same ( $1.1\text{m/s}$ ).

We also calculated the ratio of  $E_v$  for the low and high speed winds, i.e.  $E_v(V_{w0}^{low} = 1.5\text{m/s}) / E_v(V_{w0}^{low} = 0.4\text{m/s})$  and  $E_v(V_{w0}^{high} = 5.0\text{m/s}) / E_v(V_{w0}^{high} = 3.9\text{m/s})$ . As a result, the former was 1.64 and the latter was 1.14. Such values were nearly equal to the ratio of  $\alpha_v$  for the low and high speed winds, i.e.  $\alpha_v(V_{w0}^{low} = 1.5\text{m/s}) / \alpha_v(V_{w0}^{low} = 0.4\text{m/s}) = 1.61$  and  $\alpha_v(V_{w0}^{high} = 5.0\text{m/s}) / \alpha_v(V_{w0}^{high} = 3.9\text{m/s}) = 1.15$ , respectively.

#### Quasi-unsteady soil surface temperature

Attempts were made to examine the mechanism of evaporation of Eq. 2. Fig. 8 shows the time variation of  $T_{surf}$  for case A and case C from 30 to 120 minutes after the beginning of the experiment with  $\Delta t = 15$  minutes. The amplitude of  $T_{surf}$ ,  $a_{T_{surf}} (= T_{surf}^{low} - T_{surf}^{high})$ , was greater for case A than for case C. The difference in  $a_{T_{surf}}$  between case A and case C appeared mainly for the low speed wind, because the difference in  $T_{surf}^{low}$  between case A and case C,  $\Delta T_{surf}^{low}$ , was greater than the difference in  $T_{surf}^{high}$  between the two cases,  $\Delta T_{surf}^{high}$  (See the right edge of Fig. 8). This may be caused by the latent heat flux due to evaporation from the soil surface. The evidence for this assumption was obtained by the foregoing experimental result,  $\Delta E_v^{low} > \Delta E_v^{high}$  described in the section “Quasi-unsteady wind velocity and evaporation”.

Moreover,  $T_{surf}$  changed remarkably and immediately after switching the wind velocity and then asymptotically

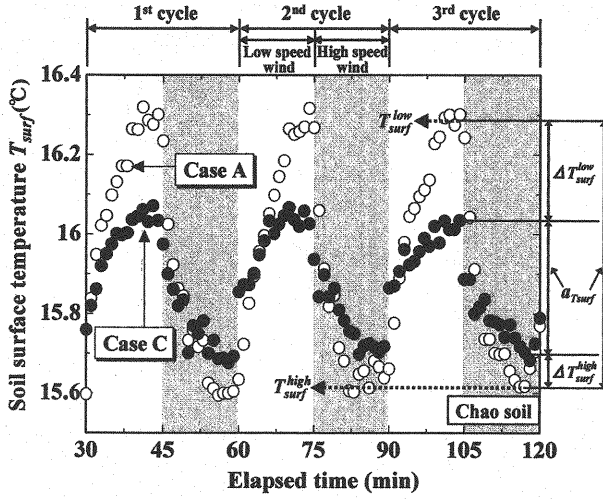


Fig. 8 Time variation of  $T_{surf}$  for C-soil from 30 to 120 minutes after beginning of the experiment (case A and case C)

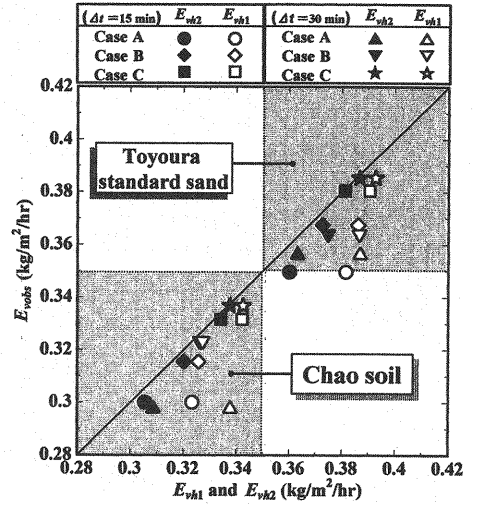


Fig. 9 Comparison of calculated HEF,  $E_{vh1}$  and  $E_{vh2}$  with observed HEF,  $E_{vobs}$

approached an equilibrium value ( $T_{surf}^{high}$  or  $T_{surf}^{low}$ ), regardless of the acceleration and deceleration (See Fig. 8). The recovery period of  $T_{surf}$  is shorter for case C (8 minutes) than for case A (10 minutes). By comparing Figs. 6 and 8, we concluded that the recovery period of  $T_{surf}$  is one order smaller than that of  $V_{w0}$ .

#### Comparison of calculated hourly evaporation flux with observed one

Fig. 9 shows the comparison of the two calculated HEF ( $E_{vh1}$  (Eq. 3) and  $E_{vh2}$  (Eq. 5)) with the observed HEF,  $E_{vobs}$ , ( $= \Sigma Q_{ev}$  at 150 minutes of the elapsed time)  $\times 60/150$ ). The results for  $\Delta t = 15$  and 30 minutes are shown together in Fig. 9.  $E_{vh2}$  can reproduce  $E_{vobs}$  better, compared with  $E_{vh1}$  for all experimental cases, regardless of the soil. Eq. 3 always overestimates  $E_{vobs}$  and the maximum error between  $E_{vh1}$  and  $E_{vobs}$  was 8% and 12% for T-soil and for C-soil, respectively. On the other hand, the maximum error between  $E_{vh2}$  and  $E_{vobs}$  was 3% and 4% for T-soil and for C-soil, respectively. The error regarding  $E_{vh2}$  may result from neglecting the time variation of  $V_{w0}$  or  $T_{surf}$  during the recovery period. However, it is clear that  $E_{vh2}$  leads to a better prediction than  $E_{vh1}$ .

Case A (● and ○, ▲ and △), with large  $\Delta V_{w0}$  and small  $V_{w0}^{low}$  ( $< 1.0$  m/s), shows a large difference between  $E_{vh1}$  and  $E_{vh2}$ . In contrast, when  $V_{w0}^{low}$  is greater than 1.5 m/s, the difference between  $E_{vh1}$  and  $E_{vh2}$  becomes small (see the result of case C (■ and □, ★ and ☆)).

As for case B and case C of the C-soil and case A and case C of the T-soil,  $E_{vobs}$  for  $\Delta t = 30$  minutes was slightly greater than that for  $\Delta t = 15$  minutes. However, by taking the experimental accuracy into account, the difference in  $E_{vobs}$  described above may be disregarded.

Finally, the overestimation of  $E_{vh1}$  may be explained as follows:

$E_{vh1}$  is calculated by inserting Eq. 4 into Eq. 3. That is

$$E_{vh1} = 3600 \alpha_v (V_{w0}^{ave}) D_{am} \left\{ \rho_{vsurf} (T_{surf}^{ave}) - \rho_{vair0} \right\} \quad (10)$$

On the other hand, the concept of  $E_{vh2}$  was in line with the change in  $E_v$  associated with  $V_{w0}$ .  $E_{vh2}$  was, therefore, in good agreement with  $E_{vobs}$ . Inserting Eqs. 6 and 6' into Eq. 5 yields the following equation.



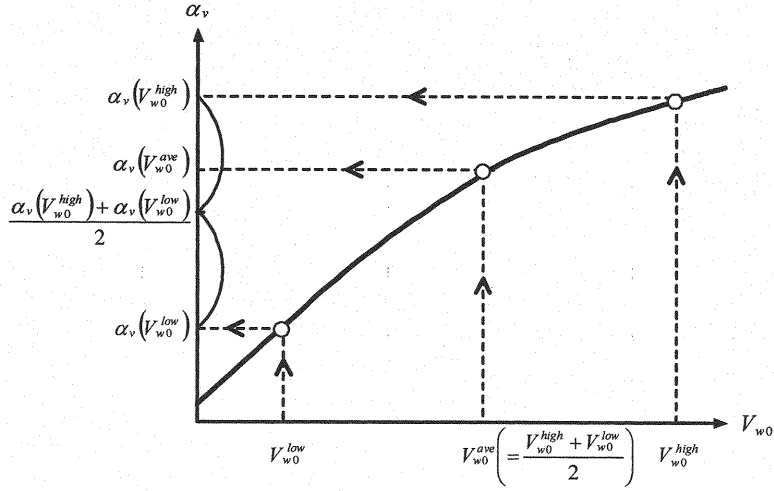


Fig. 10 Schematic view of  $\alpha_v - V_{w0}$  relation and difference between  $\alpha_v(V_{w0}^{ave})$  and  $(\alpha_v(V_{w0}^{high}) + \alpha_v(V_{w0}^{low}))/2$

$$E_{vobs} \approx E_{vh2} = 3600 \left[ \frac{\alpha_v(V_{w0}^{high}) D_{atm} \{ \rho_{vsurf}(T_{surf}^{high}) - \rho_{vair0} \} + \alpha_v(V_{w0}^{low}) D_{atm} \{ \rho_{vsurf}(T_{surf}^{low}) - \rho_{vair0} \}}{2} \right] \quad (11)$$

The following approximation:  $\Delta \rho_v = \{ \rho_{vsurf}(T_{surf}^{ave}) - \rho_{vair0} \} \approx \{ \rho_{vsurf}(T_{surf}^{high}) - \rho_{vair0} \} \approx \{ \rho_{vsurf}(T_{surf}^{low}) - \rho_{vair0} \}$  allows Eqs. 10 and 11 can be rewritten as follows:

$$E_{vh1} = 3600 \alpha_v(V_{w0}^{ave}) D_{atm} \Delta \rho_v \quad (12)$$

$$E_{vobs} \approx 3600 \frac{\alpha_v(V_{w0}^{high}) + \alpha_v(V_{w0}^{low})}{2} D_{atm} \Delta \rho_v \quad (13)$$

Since  $D_{atm}$  and  $\Delta \rho_v$  in Eqs. 12 and 13 are almost constant,  $E_{vh1}$  and  $E_{vobs}$  are approximately proportional to  $\alpha_v(V_{w0}^{ave})$  and  $(\alpha_v(V_{w0}^{high}) + \alpha_v(V_{w0}^{low}))/2$ , respectively. That is

$$E_{vh1} \propto \alpha_v(V_{w0}^{ave}) \quad (14)$$

$$E_{vobs} \propto \frac{\alpha_v(V_{w0}^{high}) + \alpha_v(V_{w0}^{low})}{2} \quad (15)$$

Fig. 10 shows a schematic view of the  $\alpha_v - V_{w0}$  relation based on Fig. 5.  $\alpha_v \{ \alpha_v(V_{w0}^{high}), \alpha_v(V_{w0}^{low}), \alpha_v(V_{w0}^{ave}) \}$  corresponding to three different  $V_{w0} \{ V_{w0}^{high}, V_{w0}^{low}, V_{w0}^{ave} \}$  are given in Fig. 10. The inequality,  $\alpha_v(V_{w0}^{ave}) > (\alpha_v(V_{w0}^{high}) + \alpha_v(V_{w0}^{low}))/2$ , is obvious. Actually the value of  $\alpha_v(V_{w0}^{ave}) / \{ (\alpha_v(V_{w0}^{high}) + \alpha_v(V_{w0}^{low}))/2 \}$  is 1.08 for case A of C-soil, and is nearly equal to that of  $E_{vh1} / E_{vobs}$  ( $= 1.10$ ), calculated by Eq. 4. The error included in  $\alpha_v$  in Eq. 4 or Eq. 10 can account for the overestimation of the HEF.

## CONCLUSIONS

As a first step towards evaluating evaporation under unsteady wind velocities, the time variation of the evaporation flux by switching between high and low speed winds at intervals of 15 or 30 minutes was examined using a wind tunnel. The new evaporation model (Eq. 5) and the conventional model (Eq. 3) were compared with the hourly evaporation flux (HEF) obtained from the wind tunnel evaporation experiments using Chao soil (Silty clay loam) and Toyoura standard sand (Sandy soil).

The conclusions drawn from this study are as follows:

- (1) The difference in the HEF exceeded 10% by changing the combinations of the high and low wind velocities, regardless of the soil, although the hourly averaged wind velocity had the same value.
- (2) The conclusion (1) was obtained by the nonlinear relation between the evaporation coefficient,  $\alpha_v$ , and the free-stream wind velocity,  $V_{w0}$ . The nonlinearity of  $\alpha_v$  is especially obvious for  $V_{w0} \leq 1.5\text{m/s}$ .
- (3) Eq. 1 was no longer valid for the present evaporation experimental results if the bulk coefficient of evaporation,  $C_E$ , is constant.
- (4) The recovery period of the evaporation flux associated with the change in  $V_{w0}$  was affected by the recovery period of the soil surface temperature rather than that of the wind velocity.
- (5) The conventional model (Eq. 3) overestimates the observed HEF by 8% and 12% at the maximum for Toyoura standard sand and for Chao soil, respectively. The error of Eq. 3 results from the nonlinearity of the  $\alpha_v$ - $V_{w0}$  relation. On the other hand, the new model (Eq. 5) reduced the error of the HEF to between 1/3 and 1/4, compared with that of Eq. 3.

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## APPENDIX – NOTATION

The following symbols are used in this paper:

- $C_E$  = bulk coefficient of evaporation (-);  
 $D_{atm}$  = diffusion coefficient of vapor in air ( $m^2/s$ );  
 $E_v$  = evaporation flux ( $kg/m^2/s$ );  
 $E_{vh1}$  = hourly evaporation flux calculated by conventional model ( $kg/m^2/hr$ );  
 $E_{vh2}$  = hourly evaporation flux calculated by new model ( $kg/m^2/hr$ );  
 $(E_{vt})_{\Delta t}$  = evaporation flux for time interval  $\Delta t$  ( $kg/m^2/hr$ );  
 $E_{vobs}$  = observed hourly evaporation flux ( $kg/m^2/hr$ );  
 $n$  = switching number of wind velocity per hour;  
 $q_{a0}$  = specific humidity of air in the free-stream region ( $kg/kg$ );  
 $q_s$  = specific humidity on the soil surface ( $kg/kg$ );  
 $T_{surf}$  = soil surface temperature ( $^{\circ}C$ );  
 $u_*$  = wall-friction velocity ( $m/s$ );  
 $V_w$  = wind velocity at  $z$  ( $m/s$ );  
 $V_{w0}$  = free-stream velocity ( $m/s$ );  
 $z$  = vertical height from roughness surface ( $m$ );  
 $z_0$  = roughness length ( $m$ );  
 $a_v$  = evaporation coefficient ( $1/m$ );  
 $\Delta t$  = time interval ( $min$ );  
 $\Delta \rho_v$  = vapor density difference between soil surface and air in the free-stream region ( $kg/m^3$ );  
 $\kappa$  = Karman constant ( $= 0.4$ );  
 $\rho$  = air density ( $kg/m^3$ );  
 $\rho_{vair0}$  = vapor density of air in the free-stream region ( $kg/m^3$ );  
 $\rho_{vsurf}$  = vapor density on the soil surface ( $kg/m^3$ );  
 Superscript:  
 $ave$  = averaged;  
 $high$  = for high speed wind; and  
 $low$  = for low speed wind.