

Numerical Shape Coefficient of Shear Deformation for Beam with Rectangular Cross-Section on Phase Velocity of Transverse Elastic Waves

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1. INTRODUCTION

In this paper, numerical shape coefficient of shear deformation for a beam with rectangular cross-section is determined based on the first mode curve of the phase velocity for transverse elastic waves obtained from Timoshenko [1].

2. PHASE VELOCITY

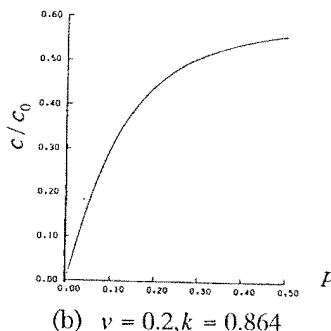
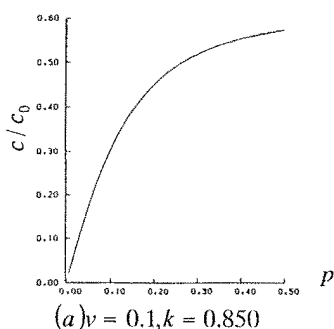
The first mode curve of phase velocity obtained from Timoshenko Beam Theory [2] can be found as follows.

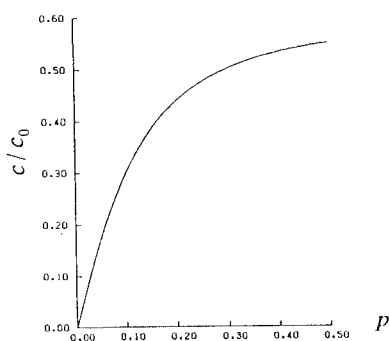
$$\frac{c}{c_0} = \frac{2\sqrt{\frac{2}{3}}(\pi p)}{\left[1 + \frac{4}{3}(a+1)(\pi p)^2 + \left\{1 + \frac{8}{3}(a+1)(\pi p)^2 + \frac{16}{9}(a-1)^2(\pi p)^4\right\}^{\frac{1}{2}}\right]^{\frac{1}{2}}} \quad (1)$$

where $c = \frac{\omega}{\gamma}$, $c_0 = \sqrt{\frac{E}{\rho}}$, $\gamma = \frac{2\pi}{\lambda}$, $a = \frac{E}{kG} = \frac{2(1+\nu)}{k}$, $p = \frac{h}{\lambda}$, c = phase velocity, ω = angular frequency, γ = wave number of transverse elastic waves, λ = wave length of transverse elastic waves, E = modulus of longitudinal elasticity of the beam, G = modulus of shear deformation, ν = Poisson's ratio, ρ = density, k = numerical shape coefficient of shear deformation, h = height of rectangular cross-section.

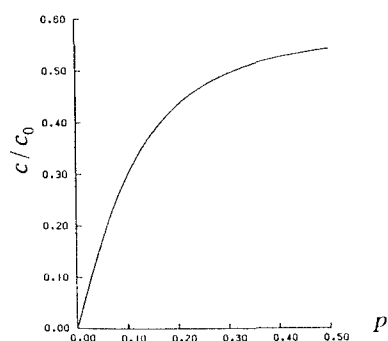
3. COMPUTATIONS

In Figure 1, results of the present authors' computations according to plane stress of two-dimensional elastic theory [1] are compared with those according to Timoshenko's theory. The real line is the first mode curve of phase velocity obtained from plane stress of two-dimensional elastic theory, and the dotted line is that obtained from Timoshenko Beam Theory. In each case of (a)-(f), giving the numerical value of ν first, computations have been repeated untill a suitable value of k is found out with which two lines well coincide with each other, by changing the value of k little by little.

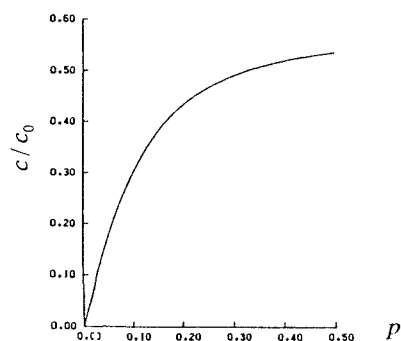




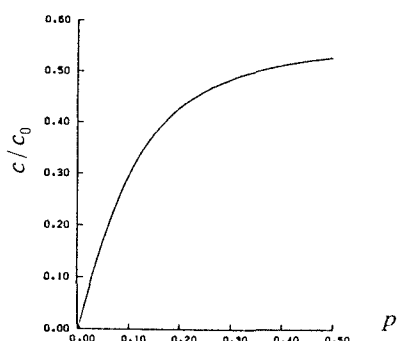
(c) $\nu = 0.25, k = 0.870$



(d) $\nu = 0.30, k = 0.875$



(e) $\nu = 0.35, k = 0.880$



(f) $\nu = 0.40, k = 0.885$

Figure 1. First mode curves of phase velocity computed from plane stress of two-dimensional elastic theory and Timoshenko's theory

4. CONCLUSIONS

Numerical shape coefficient of shear deformation for a beam with rectangular cross-section depends on Poisson's ratio. For the suitable k , the real line and the dotted line well coincide with each other.

REFERENCES

1. S. P. TIMOSHENKO 1922 Philosophical Magazine and Journal of Science 43,125-131 On the Transverse Vibrations of Bars of Uniform Cross-Section.
2. S. P. TIMOSHENKO 1921 Philosophical Magazine and Journal of Science 41,744-746. On the Correction for Shear of the Differential Equation for Transverse Vibrations of Prismatic Bars.