# EFFECT OF BUNDLING OF MULTIPLE AIRPORTS WITH TRIP－CHAIN FORMATION 

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#### Abstract

In this study，an optimization model is developed to simulate air transport market in different situations． In the model，objectives of market participant，involving airports，airlines and passengers are formulated and interactions between them are simulated．Decisions of each participant are optimized by payoff maxi－ mization endogenously and final outcome of the market is evaluated．Trip－chain passengers with multiple destinations to visit during one journey are specifically considered，their possible moving modes are gen－ erated by a shortest path sub－model．Airport bundling in Hokkaido，a plan that will be carried out with 2020 ，is taken as an example for case study．The effect is analyzed and discussed through comparison between market participants＇decision－making and final outcome before and after bundling．


Key Words ：airports bundling，airports privatization，trip－chain

## 1．INTRODUCTION

Airports were traditionally owned and operated by public sectors．However，since the first major case took place in the United Kingdom in 1987，airport privatization has become a worldwide trend ${ }^{1)}$ ．Take Japan for example，since the first privatization that took place in Narita airport in 2004，until now， 5 air－ ports have been fully or partially privatized and more future privatizations have been planned ${ }^{2}$ ．

In Japan，airport privatization is expected to have positive ripple effect．Financial independence and in－ tegrated operation of aeronautical and non－aeronauti－ cal facilities allows revenue allocation inside airport， improves economic health and enables the levy of lower airport usage fee．Lower airport usage fee strengthens competitiveness of airport and attracts the establishment of more airways and flights．In－ creasing demand then promotes the development of local economy．

Among privatization cases and schemes of Japa－ nese airports，Hokkaido scheme draw more attention． The integrated privatization of multiple distant air－ ports in one region is called bundling．In addition to the mentioned positive effect，enlargement of flights
and airways inside region and increase of trip－chain travel demand are also expected．Bundling allows co－ ordination of price setting between airports and stim－ ulate airlines to employ friendlier airway pattern，air－ fare and frequency inside the region for travelers， thus it is considered to raise the trip－chain demand， create more local consuming and make greater con－ tribution to the local economy．

However，expected positive effect of privatization will not always come．There are some examples of failure and argument about privatization from various perspective haven＇t stopped from the beginning． Moreover，there are few studies focusing on bundling case．Thus，this study aims to analyze the effect of airport bundling involving：（a）How will airports op－ timize their strategy when their decision－making modes change？（b）How will airlines and travellers respond and change their decision according to the modified strategy of airports？（c）Will these changes eventually benefit the whole industry and region？To clarify these effects theoretically，an optimization model is developed to simulate interaction between and decision－making of each participant and obtain final outcome of the air transportation market．The
proposed model is then used to analyze possible ef－ fect of airports－bundling in Hokkaido，an actual plan that will be carried out within 2020，through the com－ parison of simulated decisions of market participants and outcome before and after bunding．

## 2．METHODOLOGY

## （1）Basic configuration

## a）Air transportation market

In this study，air transport market is modelled to be composed of three types of participants：airports，air－ lines and passengers．Each participant has its own ob－ jective．Each participant attempts to achieve its ob－ jective by making decision，but desired outcome of objective cannot be realized independently，for the outcome of each participant is not only affected by its own decision，but also by decisions of others．Thus， outcome is determined by the interactions between participants：how one is affected by others＇decisions and how one＇s decisions affect others．Airports，the up－stream leader of market，will make decision at first，they set charge to airlines and passengers con－ sidering their reaction for the purpose of profit or so－ cial surplus maximization．Receiving charge from airports，the mid－stream follower，airlines，will set airway pattern，airfare and frequency for the purpose of profit maximization，considering passengers＇ac－ ceptance．At last，as down－stream followers，consid－ ering charge from airport and tactics of airlines，po－ tential passengers decide their destination choice，air－ line choice and route choice．（Fig．1）


Fig． 1 Diagram of air transport market

## b）Assumptions

## General settings

Every market participant is rational and attempts to maximize its payoff．Demand for flight service is independent from commercial activities ${ }^{3)}$ and con－ sumer surplus derived from commercial activities is not taken into account．
Airports
There are public and private airports．Charges of
public airports are predetermined by government，the charges exactly cover the operating cost to ensure air－ ports＇minimum necessary operation．Charges of pri－ vate airports are set to maximize profit or social sur－ plus in some cases．

## Airlines

There are multiple airlines competing with each other with collusion．Airlines have the freedom to adopt any kinds of airway pattern，airfare and fre－ quency only between distant airports．

## Passengers

There are two types of passengers／travellers：one－ way travellers and trip－chain travellers．One－way travellers have fixed origin and destination．Trip－ chain travellers will determine their destination based on travel utility．They can visit multiple destination during one journey and return to origin．Both type of travellers will only choose paths with fewest sections （e．g．if there are direct routes between A and B，trav－ ellers setting out from $A$ visiting $B$ will not transit in other sites）．Land transportation is available when distance between origin and destination is not so long．Ignore the factor of congestion cost．

## c）Framework

The model simulates interactions between and de－ rives optimal decisions of each participants in a back－ ward thinking，regarding the market as a Stackelberg competition．Each participant makes decision consid－ ering possible optimal response of its follower．The general description of the model is shown in Table 1.

Table 1 General description of the model

| Input paran |  |
| :---: | :---: |
| Demand | Number of potential demand，passengers＇sensitivity parameter of monetary and time cost，log－sum |
| Airline | Operating cost，attribute of aircrafts |
| Airport | Operating cost，concession revenue per passenger |
| Others | Attribute of sites，air routes and land routes，parameter of logit model，attractiveness value of destinations |
| Variable | Optimization problem |
| Demand $\mathbf{x}$ | ${ }^{\text {Airports }} \max _{T} \gamma\left(\mathbf{T}, \mathbf{f}_{i}, \mathbf{x}_{i}\left(\mathbf{p}_{i}, \mathbf{f}_{i}, \mathbf{T}\right)\right)$ |
| Airfare p |  |
| Frequency f | Where $\mathbf{p}_{i}=\left[\begin{array}{ll} \mathbf{p}_{h} & \mathbf{p}_{-h} \end{array}\right] \mathbf{f}_{i}=\left[\begin{array}{ll} \mathbf{f}_{h} & \mathbf{f}_{-h} \end{array}\right]$ |
| Charge T | Airlines $\mathbf{p}_{h}, \mathbf{f}_{h}=\underset{\mathbf{p}_{h}, \mathbf{f}_{h}}{\arg \max _{h}} \pi_{h}\left(\mathbf{p}_{h}, \mathbf{f}_{h}, \mathbf{x}_{h}\left(\mathbf{p}_{h}, \mathbf{f}_{h}, \mathbf{p}_{-h}, \mathbf{f}_{-h}, \mathbf{T}\right), \mathbf{T}\right)$ |
| Outcome |  |
| Optimal value of decision variables：demand，airlines＇airfare and frequency，airports＇charge，profit of airlines，profit of airports，consumer surplus，social surplus |  |

## （2）Model formulation

## a）Formation of trip－chains and moving modes

Given a set of sites $\mathrm{V}=\left\{v_{1}, v_{2}, \cdots, v_{n}\right\}$ and con－ nectivity between each sites pair．For travelers who set out from origin site $s$ ，visit a series of sites $\mathrm{R}=$
$\left\{r_{1}, \cdots, r_{m}\right\}$ and then return to $s$ ．For one－way travel－ ers，possible moving modes can be derived through Yen＇s algorithm ${ }^{4}$ ．For trip－chain travellers，possible moving modes are obtained by following method：

1．Create adjacency matrix $A$ of vertex（sites）set $V$ ． Then set value $A_{i j}$ to 1 if site $v_{i}$ and $v_{j}$ are con－ nected，otherwise set $A_{i j}$ to $\infty$ ．

2．List all possible sites visiting sequences of the journey，by calculating the permutation of all ele－ ments of visiting sites series R．Besides，remove se－ quences symmetric with others．Here，$Q$ and $Q^{\prime}$ are regarded＇symmetric＇if，for all $k \in \mathrm{M}$ ，the element $q_{k}$ of sequence vector $Q$ is equal to the element $q_{m+1-k}^{\prime}$ of sequence vector $Q^{\prime}$ ．For example，when $\mathrm{R}=\{2,3,4\}$ ，all possible permutations are $\{2,3,4\}$ ， $\{2,4,3\},\{3,4,2\},\{4,3,2\},\{3,4,2\},\{2,4,3\}$ ．Removing symmetric ones，final possible sites visiting se－ quences are $\{2,3,4\},\{2,4,3\},\{3,4,2\}$ ．

3．Create dummy graph $\bar{G}$ of V for each sequence $Q$ ．The matrix $\bar{A}$ of $\bar{G}$ has a shape of the block diago－ nal matrix of $\mathrm{m}+1 A$ matrices，while all 0 elements are set to $\infty$ except elements $\bar{A}\left(q_{k}+n(k-1), q_{k}+\right.$ $n k)$ and $\bar{A}\left(q_{k}+n k, q_{k}+n(k-1)\right)$ for all k．For example：when $\mathrm{V}=\{1,2,3,4\}$ ，$A=$ $\left[\begin{array}{cccc}\infty & 1 & 1 & \infty \\ 1 & \infty & 1 & 1 \\ 1 & 1 & \infty & 1 \\ \infty & 1 & 1 & \infty\end{array}\right]$ ，origin site $s$ is 1 and sequence $Q$ is $(2,3)$ ，the matrix $\bar{A}$ of dummy graph $\bar{G}$ where $\bar{A}(2,6), \bar{A}(6,2), \bar{A}(7,11), \bar{A}(11,7)$ remain as 0 is：

$$
\bar{A}=\left[\begin{array}{cccccccccccc}
\infty & 1 & 1 & \infty & \infty & \infty & \infty & \infty & \infty & \infty & \infty & \infty \\
1 & \infty & 1 & 1 & \infty & 0 & \infty & \infty & \infty & \infty & \infty & \infty \\
1 & 1 & \infty & 1 & \infty & \infty & \infty & \infty & \infty & \infty & \infty & \infty \\
\infty & 1 & 1 & \infty & \infty & \infty & \infty & \infty & \infty & \infty & \infty & \infty \\
\infty & \infty & \infty & \infty & \infty & 1 & 1 & \infty & \infty & \infty & \infty & \infty \\
\infty & 0 & \infty & \infty & 1 & \infty & 1 & 1 & \infty & \infty & \infty & \infty \\
\infty & \infty & \infty & \infty & 1 & 1 & \infty & 1 & \infty & \infty & 0 & \infty \\
\infty & \infty & \infty & \infty & \infty & 1 & 1 & \infty & \infty & \infty & \infty & \infty \\
\infty & \infty & \infty & \infty & \infty & \infty & \infty & \infty & \infty & 1 & 1 & \infty \\
\infty & \infty & \infty & \infty & \infty & \infty & \infty & \infty & 1 & \infty & 1 & 1 \\
\infty & \infty & \infty & \infty & \infty & \infty & 0 & \infty & 1 & 1 & \infty & 1 \\
\infty & \infty & \infty & \infty & \infty & \infty & \infty & \infty & \infty & 1 & 1 & \infty
\end{array}\right]
$$

Fig． 2 shows an intuitive expression of the dummy graph $\bar{G}$ ．


Fig． 2 Image of dummy graph

4．Use Yen＇s algorithm ${ }^{4)}$ to find out single or mul－ tiple shortest paths $P_{Q}^{1}, \cdots, P_{Q}^{h}$ from origin site $s$ to destination $d$ for each sequence $Q . d$ is actually the clone point of $s$ in the farthest side of dummy graph （e．g．1＇＇in figure 1）with a site index $s+n m$ ．Re－ store the remaining indexes by subtracting the ele－ ments of P that are greater than $n$ repeatly until no elements are greater than $n$ ．Remove the overlapping indexes．（e．g．in the example above，untreated short－ est path result is $P=(1,2,6,7,11,9)$ ，by restoring， $P=(1,2,2,3,3,1)$ ，by removal，$P=(1,2,3,1)$ ．）

5．For each path，obtain all possible moving mode， that means，the combination of which transport mode to use in each segment of the path．For each segment $p_{i}-p_{i+1}$ ，generate a vector $\mathbf{t}_{p_{i} p_{i+1}}=[1,2, \cdots, l]$ of all possible transportation modes including the choice of airline companies．Then，solve the combination prob－ lem of taking one element from each vector．Use the example above，if $\mathbf{t}_{12}=[1,2], \mathbf{t}_{23}=[1,2,3], \mathbf{t}_{31}=$ ［1］，all possible 6 moving modes for path P is listed as：
$d_{1}^{P}=(1,1,1) \quad d_{2}^{P}=(2,1,1) \quad d_{3}^{P}=(1,2,1)$ $d_{4}^{P}=(2,2,1) \quad d_{5}^{P}=(1,3,1) \quad d_{6}^{P}=(2,3,1)$
For each mode $d$ of each path，create a 3－dimensional cost matrix C with $l$ pages（the third dimension） where $l$ is the number of transportation modes for the path．if $d_{i j}=t$ ，set $C(i, j, t)=1$ ，otherwise 0 ．Note that if a path includes more than one segment be－ tween two sites to be visited，and the moving modes （actually airline company）for these segments are same，set corresponding elements of cost matrix to discount rate，which is for connecting flight．

## b）Demand function

Logit formulation is adopted to derive the demand of each alternatives ${ }^{5)}$ ．In the case of one－way travel－ ler，based on disutility perception of the trip，there are two phases of decision－making．At first，one needs to decide whether to take the trip（phase i）．Then，for travelers determining to take the trip，next decision to make is which airline／route to choose（phase j）．$V_{O D_{-} j}$ （Eq．（1））denotes the deterministic utility of each route $w$ of each OD．$p, t, d l, l y$ denote transport fee， travel time，schedule delay time and lay－over time re－ spectively ${ }^{6}$ ．Monetary and time cost of each alterna－ tive（moving mode）is derived through its 3－dimen－ sional cost matrix C．The demand $N_{O D_{-} j}$ of each route w of each OD is derived as Eq．（2）～（4）．

$$
\begin{align*}
& V_{O D_{-} j} \\
& \qquad-\theta\left(p_{O D_{-} j}+\alpha t_{O D_{-} j}+\beta\left(d l_{O D_{-} j}+l y_{O D_{-} j}\right)\right)  \tag{1}\\
& \Gamma_{O D_{-} Y}=\mu \ln \left(\sum_{j^{*} \in J} \exp \left(\frac{1}{\mu} V_{O D_{-} j^{*}}\right)\right)  \tag{2}\\
& N_{O D_{-} Y}=N_{O D} \exp \left(\Gamma_{O D_{-} Y}\right) \tag{3}
\end{align*}
$$

$$
\begin{equation*}
N_{O D_{-} j}=N_{O D_{-} Y} \frac{\exp \left(\frac{1}{\mu} V_{O D_{-} j}\right)}{\sum_{j^{*} \in J} \exp \left(\frac{1}{\mu} V_{O D_{-} j^{*}}\right)} \tag{4}
\end{equation*}
$$

In the case of trip－chain travelers，there are four phases of decision－making．At first，one decides whether to join the journey（phase i）．Then，for pas－ sengers determining to join the journey，they will consider destination then（phase j）．After determining destination，they need to think about transportation mode for moving（phase k）．Finally，passengers will decide detailed trip－chain（mode）（phase r）for their journey．The demand $N_{r}$ of each trip－chain r is de－ rived as Eq．（5）～（10）．

$$
\begin{gather*}
V_{r}=-\sigma\left(p_{r}+\alpha t_{r}+\beta\left(d l_{r}+l y_{r}\right)\right)  \tag{5}\\
\Gamma_{k}=\frac{\mu_{k}}{\mu_{j}} \ln \left(\sum_{r^{*} \in R} \exp \left(\frac{1}{\mu_{k}} V_{r^{*}}\right)\right)  \tag{6}\\
\Gamma_{j}=\frac{\mu_{j}}{\mu_{i}} \ln \left(\sum_{k^{*} \in K} \exp \left(\Gamma_{k}\right)\right)+\frac{1}{\mu_{i}} A t_{j}  \tag{7}\\
\Gamma_{i}=\mu_{i} \ln \left(\sum_{j^{*} \in J} \exp \left(\Gamma_{j}\right)\right)  \tag{8}\\
N_{i j k}=  \tag{9}\\
N \frac{\exp \left(\Gamma_{i}\right)}{1+\exp \left(\Gamma_{i}\right)} \frac{\exp \left(\Gamma_{j}\right)}{\sum_{j^{*} \in J} \exp \left(\Gamma_{j^{*}}\right)} \frac{\exp \left(\Gamma_{k}\right)}{\sum_{k^{*} \in K} \exp \left(\Gamma_{k^{*}}\right)}  \tag{10}\\
N_{r}=N_{i j k} \frac{\exp \left(\frac{1}{\mu_{k}} V_{r}\right)}{\sum_{r^{*} \in R} \exp \left(\frac{1}{\mu_{k}} V_{r^{*}}\right)}
\end{gather*}
$$

As a result，demand of air route $\rho$ of airline com－ pany $\mathrm{h} x_{h l}$ can be can be derived as shown in Eq． （11）．$\delta_{O D j h \rho}$ is a binary variable that equals 1 when trip w of OD contains route $\rho$ of airline h，and 0 oth－ erwise．$\delta_{r h \rho}$ equals 1 if trip－chain r contains route $\rho$ of airline h ，and 0 otherwise．

$$
\begin{equation*}
x_{h \rho}=\sum_{O D} \sum_{w} N_{O D_{-} i} \delta_{O D i h \rho}+\sum_{r} N_{r} \delta_{r h \rho} \tag{11}
\end{equation*}
$$

## c）Airline＇s profit maximization

The profit of airline h is defined as profit from flight services，as shown in Eq．（12）．In RHS，first term denotes revenue generating from airfare， $\mathbf{p}_{h}, \mathbf{x}_{h}$ is the vector of airfare set by airline $h$ and traffic de－ mand of airline $h$ in each airway，respectively．second term denotes aircraft operating cost． $\mathbf{f}_{h}, \mathbf{s}_{h}$ is the vec－ tor of frequency set by airline h and the seating ca－ pacity of aircraft of airline $h$ in each airway，respec－ tively． $\mathbf{D}$ is the diagonal matrix of airway distance of each airway link $d_{l}, c_{h}$ denotes unit cost of airline $h^{7)}$ ．Third term denotes charge from airports． $T\left(\mathbf{w} \mathbf{g}_{h}\right)$ is the mapping of maximum landing weight of aircraft of airline $h$ in each airway $\mathbf{w g}_{h}$ ，denotes the charge that airline needs to pay flying each link，
which is the summation of the charge from two end－ point airport of the link．

$$
\pi_{h}=\mathbf{p}_{h}^{\mathrm{T}} \mathbf{x}_{h}-2 c_{h} \mathbf{f}_{h}^{\mathrm{T}}\left(\mathbf{D} \mathbf{s}_{h}\right)-\mathbf{f}_{h}^{\mathrm{T}} T\left(\mathbf{w} \mathbf{g}_{h}\right)
$$

$$
\begin{equation*}
\forall h \in H \tag{12}
\end{equation*}
$$

Airlines respond to charges from airports and com－ pete in duopolistic airline market，by optimizing their own frequency（airway pattern）and airfare（Eq． （13））． $\mathbf{p}_{-h}, \mathbf{f}_{-h}$ are matrixs of airfare and frequency of each link／route of other airlines besides $h$ ． $\mathbf{T}$ is the vector of landing fee of each airport．Capacity con－ straint that，passenger flow on every link should not exceed the total seat capacity offered，needs to be sat－ isfied（Eq．（14））．

$$
\begin{array}{ll}
\max _{\mathbf{p}_{\mathbf{h}}, \mathbf{f}_{\mathbf{h}}} \pi_{h}\left(\mathbf{p}_{\mathbf{h}}, \mathbf{f}_{\mathbf{h}}, \mathbf{p}_{-\mathbf{h}}, \mathbf{f}_{-\mathbf{h}}, \mathbf{T}\right) & \forall h \in H \\
\text { s.t. } f_{h l} S_{h l} \geq x_{h l} \quad \forall h \in H & \forall l \in L \tag{14}
\end{array}
$$

## d）Airport＇s profit maximization

The profit of airport $a$ is defined as Eq．（15）．First term of RHS refers to aeronautical profit generating from landing fee． $\mathbf{f}_{a}$ is the vector of frequency of each aircraft type landing on airport $a . \mathbf{T}_{a}$ is the vec－ tor of charge to set to each aircraft type landing on airport $a . \mathbf{c}_{a}$ is the vector of marginal operating cost per flight landing of each aircraft type of airport $a$ ． Second term refers to concession profit generating from commercial activities．$p t_{a}$ and $z_{a}$ denote the average non－aeronautical profit from per visitor and number of visitors of airport $a$ ，respectively．

$$
\begin{equation*}
\gamma_{a}=\mathbf{f}_{a}^{\mathrm{T}}\left(\mathbf{T}_{a}-\mathbf{c}_{a}\right)+p t_{a} z_{a} \quad \forall a \in A \tag{15}
\end{equation*}
$$

When airports are bundled，suppose that the new private operator will optimize charge of each airport for the purpose of maximizing gross profit of all air－ ports subject to slot constraint（Eq．（16）～（17））． When setting charge，airport will consider the opti－ mal response of downstream market in order to get maximum payoff．

$$
\begin{align*}
& \max _{\mathbf{T}} \sum_{a} \gamma_{a}(\mathbf{f}, \mathbf{x}, \mathbf{T})  \tag{16}\\
& \text { s. t. } \sum_{h} f_{h a} \leq S_{a} \quad \forall a \in A \tag{17}
\end{align*}
$$

## e）Social surplus function

Social surplus is defined as the summation of profit of airlines，profit of airports and consumer sur－ plus，as shown in Eq．（18）．Consumer surplus is shown in Eq．（19）as the summation of consumer sur－ plus of one－way passenger and trip－chain passenger． It is obtained as integral of the demand function with respect to price，from the market price to the maxi－ mum reservation price．

$$
\begin{gather*}
S S=\sum_{h} \pi_{h}+\sum_{r} \gamma_{r}+C S  \tag{18}\\
C S=\sum_{O D}\left(\int_{-\left(\Gamma_{O D_{Y}} / \theta\right)}^{\infty} N_{O D} \exp (-\theta \omega) d \omega\right) \\
+\int_{-\left(\Gamma_{i} / \sigma\right)}^{\infty} N \frac{\exp (-\sigma \omega)}{1+\exp (-\sigma \omega)} d \omega \tag{19}
\end{gather*}
$$

## （3）Solving procedure

This problem can be regarded as an optimization problem with two sub－level：airport level and airline level ${ }^{88}$ ．The brief flow chart of the problem is shown as Fig．3．


Fig． 3 Procedure of optimization
The problem of airline level can be regarded as a competition with non－cooperative collusion，a multi－ objective optimization．However，a Nash equilibrium does not necessarily exist ${ }^{9}$ ．Thus，Non－dominated Sorting Genetic Algorithm is used to obtain pareto solution of airline level ${ }^{10)}$ ．The optimization problem of outer level，airport level is solved by Particle Swarm Optimization（PSO）algorithm．

## 3．NUMERICAL COMPUTATION

## 1）Basic scenario

As case study，the effect of airport bundling in Hokkaido will be analyzed by the model．However， the computation complexity will be quite high if we consider all 7 airports involved in the actual plan and airways connecting them．Thus，some simplifications are made：seven airports are categorized into 3 types $\mathrm{B}, \mathrm{C}$ and D defined in assumption based on their at－ tribute，and each type is imagined as one single air－ port（Fig．4）．Suppose there are two airlines with sim－ ilar market power in the market and only one land
transport medthod（bus）is available．Parameters are set based on actual situation if possible．


Fig． 4 Airport group and network
Decisions of each participant and following out－ comes are optimized and simulated by three cases．In case 1 ，airports are operated and managed by govern－ ment．Airports＇charges are predetermined by MLIT homogenously．In case 2，airports are bundled．The single operator will set charge of each airport inte－ gratedly for the purpose of maximizing gross profit． In case 3，a Ramsey price，which is to maximize so－ cial surplus subject to a constraint of budget balance， will be set when bundling．Under each case，we try to perform simulations of 5 sub－cases in terms of the proportion of potential trip－chain demand in gross potential demand，from $10 \%$ to $50 \%$ ．

## 2）Result

Table 2 Optimal airport charge in each case

| Trip－chain |  | 10\％ | 20\％ | 30\％ | 40\％ | 50\％ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { O} \\ & \text { シ्ర } \\ & \text { - } \end{aligned}$ | T（B） | 16 | 16 | 16 | 16 | 16 |
|  | T（C） | 16 | 16 | 16 | 16 | 16 |
|  | T（D） | 16 | 16 | 16 | 16 | 16 |
| $\begin{aligned} & \text { O} \\ & \text { O} \\ & \text { N } \end{aligned}$ | T（B） | 1000 | 1000 | 1000 | 1000 | 1000 |
|  | T（C） | 1000 | 828 | 1000 | 1000 | 1000 |
|  | T（D） | 1000 | 1000 | 1000 | 1000 | 1000 |
|  | T（B） | 0.5 | 0 | 0.5 | 12.2 | 16.9 |
|  | T（C） | 2.6 | 13.6 | 20.9 | 0 | 0 |
|  | T（D） | 49.1 | 18 | 1.7 | 1.8 | 0 |

The results of cases are compared herein．At first， the optimal charge T of each airport is shown in Ta－ ble 2．The pre－determined public charge，which is a
piecewise charge with respect to maximum landing weight originally，is turned into the form of dollar per tonne roughly for the convenience of comparison． From the result of case 2 ，it can be observed that， without any restriction，optimal charges set by profit maximizing airports are extremely high and unrealis－ tic．This is probably because：（a）Through bundling， the new private operator becomes the only participant in local upstream market，it can fully exploit its mo－ nopoly power without any competition．（b）Airlines are not sensitive to airports＇charges，which does not play a great role in an airline＇s cost，in the perspective of balance．On average，airport charges represent a relatively small part（typically around 4 percent）of an airline＇s total operating costs ${ }^{1)}$ ．Flight operation cost usually accounts for more percentage of total op－ erating cost of an airline．Even if airport levy an ex－ tremely high charge so that charge becomes main component of an airline＇s operating cost，it is very possible for airline to ensure a positive balance．For example，when airport B sets its charge to $1000 \$ /$ ton， cost for charge will be $\$ 203200=\$ 200 * 100(\$ /$ ton $)+$ $\$ 3200$ when an airline operate one flight on air route （A＝B），flight operation cost will be $\$ 53400=$ $0.08(\$ / \mathrm{km}$ seat）$* 890(\mathrm{~km}) * 375($ seat $) * 2$ ．Total cost will be $\$ 256600=\$ 203200+\$ 53400$ ．Revenue can exceed total cost as long as airline set an one－way air－ fare over $\$ 342=\$ 256600 /(375 * 2)$ ensuring flight to be fully loaded．In reality，however，when charges go extremely high，an airline might retreat from current market and seek a more profitable market to allocate its resource in a more efficient way，instead of endur－ ing the high charges．While in this study，only one market is assumed，there are no other substitute mar－ kets，so airline will hold on as long as it can make profit．

From the result of case 3，it can be observed that optimal charges under Ramsey pricing are generally lower than the public charges predetermined by gov－ ernment．Moreover，pricing coordination between airports in response to different trip－chain demand proportion can be observed：When trip－chain demand becomes higher，charges of airport C and D become lower while charge of airport B becomes higher． That＇s just the effect expected to be realized through integrated operation．When managed by government， charges of various airports are set to same level de－ spite their distinctive situations．The unreasonable homogenous charging might cause surplus loss sometimes．For example，the charging rules of Haneda，New Chitose and Wakkanai are completely same．Thanks to high demand，Haneda and New Chi－ tose can keep profitable with that charge．The decent financial room generating from profitable operation and the huge potential demand make it possible for two airports to lower charges further．By doing so，
higher social surplus from increasing demand can be expected without the concern of deficit．On the other hand，due to low demand，Wakkanai is suffering def－ icit，and it seems difficult to make some improve－ ment．However，it should be noted that demand of Wakkanai mainly generates from New Chitose and Haneda．If coordination is possible，By lowering charges of New Chitose and Haneda by 10 and raise the charge of Wakkanai by 5 simultaneously，then more traffic demand between them can be attracted because of the lower total charge of the air routes，and the economy of Wakkanai airport can also be im－ proved．Of course，the example above is an ideal case assumed，but the result generally reflects the assumed pricing coordination pattern：lower charge for higher demand，higher charge for lower demand，lower total charge of an air route compared to predetermined one．

Then，as the response of airlines to the optimal charges，the results of airlines airfare and frequency are shown in Fig． 5 and Fig．6．From the comparison by case（pricing mode），it can be observed that under profit maximizing charges（case 2），airfares are high－ est and frequencies are lowest．While under Ramsey pricing charges（case 3），airfares are lowest and fre－ quencies are highest generally．


Fig． 5 Scatter plot of the airfare


Fig． 6 Scatter plot of the frequency

Table 3 Demand，demand visiting multiple sites，consumer sur－ plus，airline profit，airport ptofit and social surplus

| Trip－chain |  | 10\％ | 20\％ | 30\％ | 40\％ | 50\％ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Case 1 | 9336 | 9337 | 9570 | 9862 | 10118 |
|  | Case 2 | 6617 | 7874 | 6873 | 6647 | 6708 |
|  | Change | －29．1\％ | －15．7\％ | －28．2\％ | －32．6\％ | －33．7\％ |
|  | Case 3 | 9675 | 9778 | 9897 | 9972 | 10201 |
|  | Change | ＋3．6\％ | ＋4．7\％ | ＋3．4\％ | ＋1．1\％ | ＋0．8\％ |
|  | Case 1 | 282 | 544 | 865 | 1170 | 1511 |
|  | Case 2 | 161 | 422 | 527 | 662 | 858 |
|  | Change | －43．1\％ | －22．5\％ | －39．0\％ | －43．4\％ | －43．2\％ |
|  | Case 3 | 302 | 591 | 890 | 1211 | 1537 |
|  | Change | ＋7．0\％ | ＋8．6\％ | ＋2．9\％ | ＋3．5\％ | ＋1．7\％ |
|  | Case 1 | 7.09 | 6.79 | 6.61 | 6.57 | 6.45 |
|  | Case 2 | 5.04 | 5.72 | 4.76 | 4.45 | 4.23 |
|  | Change | －29．0\％ | －15．7\％ | －28．0\％ | －32．3\％ | －34．4\％ |
|  | Case 3 | 7.31 | 7.09 | 6.87 | 6.59 | 6.49 |
|  | Change | ＋3．1\％ | ＋4．5\％ | ＋3．9\％ | ＋0．3\％ | ＋0．5\％ |
|  | Case 1 | 6.82 | 6.83 | 6.8 | 6.76 | 6.75 |
|  | Case 2 | 2.73 | 2.21 | 2.15 | 1.97 | 1.75 |
|  | Change | －60．0\％ | －67．6\％ | －68．4\％ | －70．9\％ | －74．1\％ |
|  | Case 3 | 6.91 | 6.9 | 6.87 | 6.86 | 6.77 |
|  | Change | ＋1．3\％ | ＋1．0\％ | ＋1．0\％ | ＋1．5\％ | ＋0．3\％ |
|  | Case 1 | 0 | 0 | 0 | 0 | 0 |
|  | Case 2 | 3.81 | 4.55 | 4.28 | 4.28 | 4.48 |
|  | Case 3 | 0.15 | 0.14 | 0.14 | 0.16 | 0.18 |
|  | Case 1 | 14.11 | 13.81 | 13.62 | 13.54 | 13.42 |
|  | Case 2 | 11.58 | 12.48 | 11.19 | 10.69 | 10.46 |
|  | Change | －18\％ | －10\％ | －18\％ | －21\％ | －22\％ |
|  | Case 3 | 14.37 | 14.14 | 13.88 | 13.61 | 13.44 |
|  | Change | ＋1．9\％ | ＋2．3\％ | ＋2．0\％ | ＋0．6\％ | ＋0．2\％ |

Table 3 shows the result of market outcome，in－ volving demand，demand visiting multiple－destina－ tion，consumer surplus，airlines＇profit，airports＇ profit and social surplus．Under profit maximizing charging when bundling，most outcomes including demand，consumer surplus，airlines＇profit and social surplus decline significantly，only airports can achieve great profit in such regime．It＇s just the con－ sequence that an unrestricted upstream leader fully exploits its monopoly power by setting self－interested charges．In contrast，if charges are set under Ramsey pricing，improvement in demand，consumer surplus， airlines＇profit and can be observed．The improve－ ment is considered to be brought by coordination of pricing between airports mentioned above．However， the improvement is not significant．About the modest improvement，a possible explanation is that，since
charge in public operating regime is not high，and air－ line＇s price sensitivity is low besides，room for im－ provement is limited．

## 4．CONCLUSION

This study developed a model to investigate the outcomes of air transportation market．In the model， participants of the market，including airports，airlines and passengers，make decisions to maximize their payoff．Charge of each airport，airway pattern of each airline，airfare and frequency of each route and de－ mand are generated endogenously through optimiza－ tion．In addition to traditional one－way demand，pos－ sible travel patterns of trip－chain passengers who might visit multiple destinations during one journey are also considered．Given the set of sites，all possible trip－chain moving modes is derived and cost of each mode is formulated to the model．The model is used to analyse the effect of airports bundling in Hok－ kaido，by comparing the possible outcome of market simulated before and after integrated privatization of multiple airports．Some assumptions and simplifica－ tions are made to ensure the feasibility and efficiency of simulation．

The result shows that improvement of market out－ come，including demand，consumer surplus and so－ cial surplus，cannot be achieved by bundling without any restriction．Under such profit maximizing re－ gime，as the leader of upstream market，the private operator will fully exploit its monopoly power to set extremely high charges，leading to great loss in mar－ ket outcome．However，through Ramsey pricing，out－ come loss can be avoided and improvement of de－ mand，airlines＇profit，consumer surplus and social surplus can be expected compared to pre－bundling re－ gime．The improvement is considered to be brought by the coordination of pricing between multiple air－ ports and indicates the necessity of pricing regulation when airports are privatized，even though room for improvement may not be large，for the charges set by public sector are not high before bundling．Effect of the introduction of passenger charge is also investi－ gated．Higher improvement might be achieved by levy of both passenger and flight landing charge，but the result can only be regarded as a rough reference due to the instability of simulation caused by in－ creased complexity．

However，the study has several limitations．First， some actual data，such as potential demand，trip－ chain behaviours of passengers and attractiveness of each destination cannot be obtained．This makes it difficult to define parameters in passenger＇s decision－ making functions and formulate passenger＇s travel－ ling pattern correctly．Some regarding survey is de－ sired to collect essential information．Second，airline
market simulated is only part of the actual one，some airlines providing low price service are ignored． Third，the simplification that imagines multiple air－ ports to one single airport in numerical computation phase leads to exaggerated potential demand of each air route．These two points cause overestimated air－ lines＇response to airports＇charge and affect the ac－ curacy and reliability of final outcome．Fourth，cur－ rent algorithm for both trip－chain moving modes for－ mation and optimaiztaion is not efficient and stable especially when number of sites（nodes）and variables increases and complexity goes up，the model itself and algorithm still need to be improved．

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