



height. Bedform steepness indicates geometric properties of sand wave and it is function of transport stage parameter or the Shields parameter  $T = (u_* / u_{*c})^2 - 1$ . Here,  $u_*$  is the bed shear velocity; and  $u_{*c}$  is the critical bed shear velocity. Figure 2 shows the bedform steepness of experimental beds along with Nordin and Algert<sup>(4)</sup> data. For Nordin and Algert<sup>(4)</sup> data average bedform height was estimated from significant dune height divided by factor of 1.5 obtained from our experimental results. Groin bedform steepness increased with increase of transport stage parameter. Steepness of no hydraulic structure bed was higher than groin beds, but less than Nordin and Algert data and maximum steepness given by Yalin<sup>(5)</sup>. Bedform steepness for Case 6 bed was almost close to no groin bed. Groin bedform steepness will further increase with increase of tractive force.

#### 4. Roughness of the experimental beds

Equivalent roughness of the experimental beds was computed by the resistance equation of hydraulic rough flow. Table 1 shows that the presence of hydraulic structures effected the equivalent roughness. The relative roughness of experimental beds which is function of bedform height and steepness is plotted along with the methods predicted by the investigators<sup>(6)</sup> (Fig. 3). It shows that bedform of groin bed is similar to no groin bed.

#### 5. Power spectrum as function of bedform height

The proportional factor of '-3 power law' for the groin beds<sup>(7)</sup> varied along with bed shear stress. Similar to ocean waves, a relationship between power spectrum and bedform height is derived from auto-correlation function for bed elevation  $Y(x)$  with lag distance  $\tau = 0$ , where  $Y$  is bed elevation and  $x$  is longitudinal distance. Jain and Kennedy<sup>(8)</sup> assumed a certain range of wave numbers  $k_1$  to  $k_n$  for fully developed bed profiles over which the mean square value of bed elevation might remain unchanged. Assuming that the mean square of dune bed elevation  $Y$  is proportional to square of the average bedform height  $H$ , the area under the spectrum density function for equilibrium sub-range of wave number  $k_1$  to  $k_n$  of the bed profile could be given by

$$\sum_{k_1}^{k_n} S(k_i) \Delta k = cH^2 \quad (1)$$

Here  $S(k)$  = power spectrum density (PSD) function,  $k$  = Wave number cycle/cm and  $c$  = proportional factor. The relation (1) gives the validity to the interpretation of wave number PSD function  $S(k)$  of longitudinal bed profile as energy spectrum. The Figure 4 shows similar relation as equation (1) with  $1.5 \times 10^{-4}$  proportional factor.

#### 6. Conclusions

Groin bedforms are similar to no groin bedform for relatively low groin height and tractive force. Bedform steepness of groin beds might further increase with increase of tractive force. Bedforms might show different result for higher groin height and larger tractive force. Similar to significant ocean waves, area under the PSD function of sand wave is related to the second power of average bedform height.

#### References

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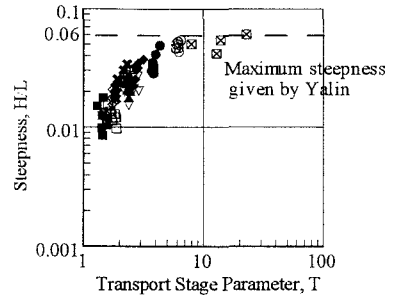


Fig. 2 Bedform steepness

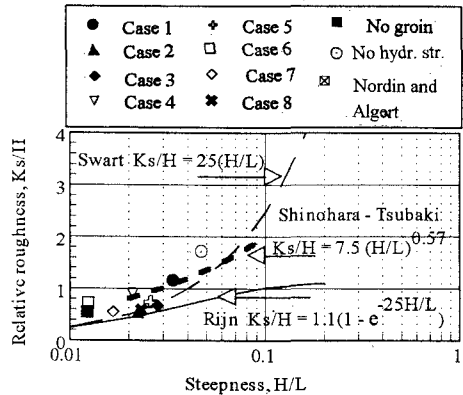


Fig. 3 Comparison of bedform roughness

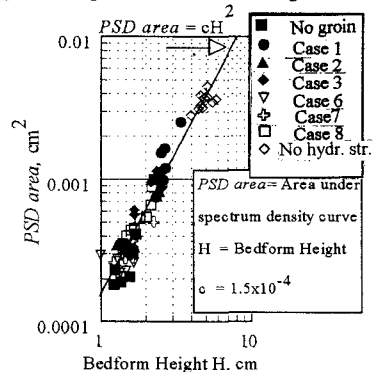


Fig. 4 Spectrum as a function of bedform height