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# FALLIBLE USE OF STIFFNESS RATIO IN CLASSIFICATION SYSTEMS

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#### 1. INTRODUCTION

The key concept used in devising non-dimensional connection classification systems [1,2] is that the initial connection stiffness  $R_{ki}$  (herein after referred to connection stiffness) can be expressed as a multiple of beam stiffness either of full length [2] or of a reference length [1] of the connecting beam. In other words, connection stiffness  $R_{ki}$  can be expressed as:

$$R_{ki} = \lambda \frac{EI}{L'} \tag{1}$$

where,

$$L' = L : EC3[2],$$
  $L' = 5d : Bjorhovde et al.[1]$  (2), (3)

and

 $\lambda$ : stiffness ratio between the connection stiffness and the beam stiffness,

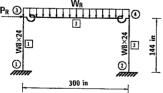
EI : flexural rigidity of the connecting beam,

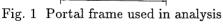
L and d: length and depth of the connecting beam, respectively.

The stiffness ratios  $\lambda$ s used to demarcate rigid and semi-rigid connection zones in EC3 classification system [2] are 25, 25/3 for unbraced and braced frames, respectively, while the counterfigure used for Bjorhovde et al's one [1] is L/2d. This study is aimed trace out the real relation between connection stiffness and beam stiffness.

# 2. ANALYSIS TECHNIQUE

A portal frame is analyzed as shown in Fig. 1. To track down the effect of the I/L ratio of the connected beam on the numerical analyses, three beam sections: W12×14, W14×22 and W14×38 for 200, 300 and 400 in beam lengths, respectively are chosen. The frame spacing is taken as 300 in. The loads applied to the frame are: uniform beam loads  $W_R = 0.0708 \ \text{kip/in}$ ,  $W_F = 0.2117 \ \text{kip/in}$  and concentrated wind loads  $P_R = 3.9 \ \text{kip}$ ,  $P_F = 7.8 \ \text{kip}$  for roof and floor beams/nodes, respectively. Wind load is applied for unbraced frame while for braced frame wind load is taken as non-existent.





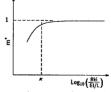


Fig. 2. Ideal  $m^*-log_{10}[R_{ki}/(EI/L)]$  curve

The procedure adopted in the frame analyses are as follows:

(1) Frame analyses are conducted taking all beam-to-column connections are rigid connections. Frame responses (beam end moment, m<sub>1</sub>) are calculated by utilizing a second-order elastic analysis program.

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- (2) Frame analyses are conducted for the same frames replacing the rigid connections with the connections correspond to EC3 [2], Bjorhovde et al. [1] and extended end-plate connections and frame responses (beam end moment, m<sub>2</sub>) are obtained. The extended end-plate connections consist of an end-plate extended beyond the beam flange(s), welded to the beam end and bolted to the column flange. A total of 112 extended end-plate connections are utilized in this analysis. On the other hand, the moment-rotation curves for the connections corresponding to the classification systems are prepared based on the prescribed moment-rotation relations.
- (3) From the results of frame analyses,  $m^* \log_{10}[R_{ki}/(EI/L)]$  figures are plotted, where  $m^*$  is obtained from:  $m^* = m_1 / m_2$ .
- (4) Steps (1) to (3) are repeated for different values of beam lengths.

# 3. DISCUSSION ON RESULTS OF FRAME ANALYSES

An ideal  $m^* - \log_{10}[R_{ki}/(EI/L)]$  figure has been drawn in Fig. 2 based on the results of the frame analysis which reveals that data representing the extended end-plate connections are distributed in the vicinity of  $m^*=1$  line on the right hand part of a certain vertical line  $\log_{10}[R_{ki}/(EI/L)] = \kappa$ . Since, the nodal moments of the frames with real connections are nondimensionalized with reference to those of fully rigid connections,  $m^*=1$  for a particular connection obviously means that the connection behavior has sufficient resemblance with that of fully rigid connection. Therefore, a rigid connection zone is defined with the following equation:

$$0.90 \le \text{m}^* \text{ for } \log_{10}[R_{ki}/(\text{EI/L})] \ge \kappa$$
 (5)

With the aid of this definition, the values of  $\kappa$  for different nodes of the frames are determined in such a manner so that most of the experimental data lie in the rigid connection zone of  $m^* - \log_{10}[R_{ki}/(EI/L)]$  figures. It is obvious that stiffness ratio  $\lambda$  can be expressed as:  $\lambda = 10^{\kappa}$ . Therefore, obtaining a series of  $\kappa$  from moment analyses, a summerized list of  $\lambda$  is presented in Table 1. This table reveals that the value of stiffness ratio  $\lambda$  varies considerably with the variation of I/L ratio of the connecting beam. This goes contrary to the EC3 [1] proposition that connection stiffness can be expressed as a constant multiple of beam stiffness. Since stiffness ratio  $\lambda$  correspond to Bjorhovde et al.'s classification [1] are expressed in terms of L/d, corresponding values shown in Table 1 reflect obvious inconsistency.

Length L (in) I/L (in <sup>3</sup>		Value of stiffness ratio $\lambda$						
	T/I (in <sup>3</sup> )	Unbraced			Braced			
	1/D (III )	Present study	EC3 [4]	Bjor. [3]	Present study	EC3 [4]	Bjor. [3]	
200	0.443	28.2	25	8.4	11.5	8.3	8.4	
300	0.663	19.9		10.9	11.2		10.9	
400	0.963	17.8		14.2	9.1		14.2	

Table 1 List of stiffness ratio  $\lambda$  from frame analysis (node 3)

# 4. CONCLUSION

Showing a significant disagreement with the classification systems, the frame analysis conducted in this study reveals that the connection stiffness can not be expressed as a constant multiple of beam stiffness. Therefore, the use of stiffness ratio between connection and beam in devising connection classification system is fallible.

#### REFERENCES

<sup>[1]</sup>Bjorhovde, R., Colson, A. and Brozzetti, J. (1990), "Classification System for Beam-to-Column Connections", Journal of ASCE, 116 (ST11), pp. 3059-3076.

<sup>[2]</sup>EC3 Code (1992), Design of Steel Structures, Part 1.1, European Committee for Standardization, CEN, Brussels.