

I - A78 CYCLIC INELASTIC SECTIONAL BEHAVIOR OF STEEL MEMBERS

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INTRODUCTION: The present paper is concerned with the cyclic inelastic sectional behavior of steel members subjected to the combined axial force and bending moment. For this purpose, a two surface model in force space (2SM-FS)^{1),2)} has recently been developed by extending the basic assumptions used in the two surface model in stress space (2SM-SS)³⁾. First, the procedure for determining of the model parameters is described. Then, the accuracy of the 2SM-FS is verified by comparing the cyclic sectional behavior of steel members obtained from the 2SM-FS with those of the direct integration method using 2SM-SS and experiments.

CONCEPT OF 2SM-FS: The 2SM-FS is based on the assumptions of no distortion of the cross section and only normal stress acting on the cross section. As shown in Fig. 1, in the non-dimensional axial force $n (= N/N_y)$ and bending moment $m (= M/M_y)$, the 2SM-FS is described by the loading (yield) curve which, initially, coincides with the initial yield curve F_0 defined by:

$$F_0(m, n) = |m| + |n| - 1 = 0 \quad (1)$$

The loading curve progressively changes in shape analogous to that of the yield plateau curve F_y defined by:

$$F_y(m, n) = \left(\frac{m}{f_y}\right)^{c_1} + n^{c_2} - 1 = 0 \quad (2)$$

and the bounding curve F_b defined by:

$$F_b(m, n, \beta_m, \beta_n, r_b) = \left(\frac{m - \beta_m}{r_b f_b}\right)^{c_3} + \left(\frac{n - \beta_n}{r_b}\right)^{c_4} - 1 = 0 \quad (3)$$

Here, N_y and M_y denote, respectively, the yield axial load and yield bending moment of the cross-section. c_1, c_2, c_3, c_4 = constant values related to the type of cross section and material; f_y, f_b = shape parameters; $r_b = \bar{R}/\kappa_0$; \bar{R} = the radius of bounding curve; κ_0 = the radius of initial yield curve; (β_m, β_n) = the coordinates of the center of bounding curve. The loading curve is always enclosed by the bounding curve and the value of plastic modulus^{2),3)} is determined by the proximity of the two curves in the course of their coupled translation and change in size and shape during plastic deformation.

MODEL PARAMETERS: The direct integration method⁴⁾ is used to determine the 2SM-FS parameters. In this approach, the section analyzed is divided into elemental areas, as shown in Fig. 2. The incremental stress-strain relation for each elemental area is described by the uniaxial 2SM-SS. The stress resultants of axial force N and bending moment M are calculated simply by summing the contribution of each elemental area over the cross-section.

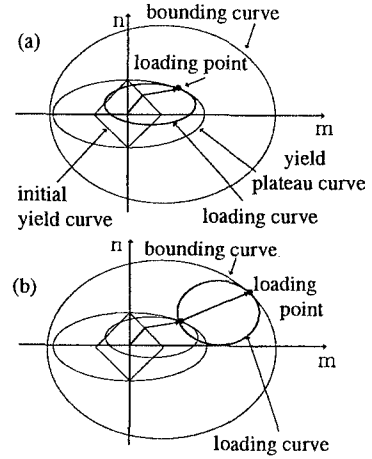
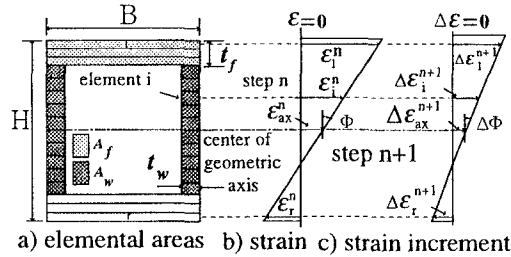


Fig. 1 Concept of 2SM-FS



a) elemental areas b) strain c) strain increment

Fig. 2 Subdivision of cross section and strain distribution for a box section

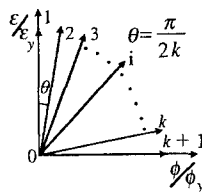


Fig. 3 Loading paths

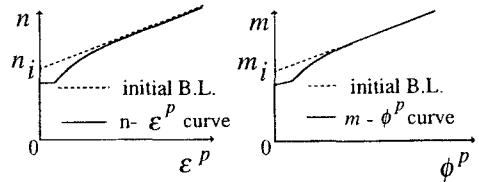


Fig. 4 Definition of initial bounding line

The axial strain and curvature, with a prescribed ratio as shown in Fig. 3, are increased incrementally and the axial force and bending moment are calculated. From the $m - \phi$ and $n - \varepsilon$ curves the values of m_i and n_i corresponding to the yield plateau and bounding curves are determined for a specific i th loading path, cross-section and material, example of which is shown in Fig. 4.

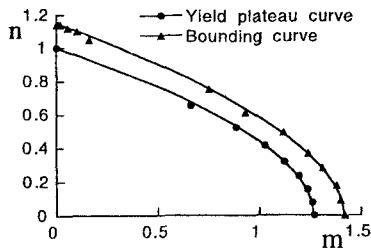


Fig. 5 Definition of the yield plateau and initial bounding curves

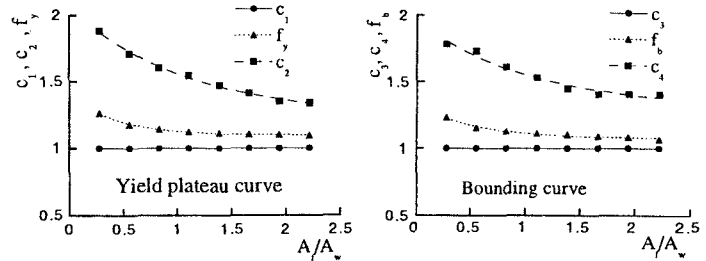


Fig. 6 2SM-FS parameters for I and box sections

The results for different loading paths are plotted in the $n - m$ coordinate system and the values of c_1 to c_4 , f_y , and f_b are determined by fitting the yield plateau and bounding curves using the least square method, as shown in Fig. 5 for a box section and SS400. The values of model parameters are examined for different sectional parameters (B/H ratio for rectangle, A_f/A_w ratio for box and I sections, and D/t ratio for a tube). The results for a typical example are shown in Fig. 6. Finally, the model parameters determined for the I and box sections corresponding to the SS400 are given in Table 1.

Table 1 2SM-FS model parameters for I and box sections (SS400)

c_1	1.0
c_2	$1.23 + 0.83 \exp\{-0.92(A_f/A_w)\}$
f_y	$1.10 + 0.31 \exp\{-2.29(A_f/A_w)\}$
c_3	1.0
c_4	$1.29 + 0.66 \exp\{-0.93(A_f/A_w)\}$
f_b	$1.08 + 0.26 \exp\{-1.92(A_f/A_w)\}$

VERIFICATION: The cyclic sectional behavior of steel members are analyzed using the 2SM-FS and the results are compared with those of the direct integration method and experiments⁴⁾. As shown in Figs. 7 and 8, a good correlation between the two analytical methods and experiments are achieved indicating the accuracy of the 2SM-FS model.

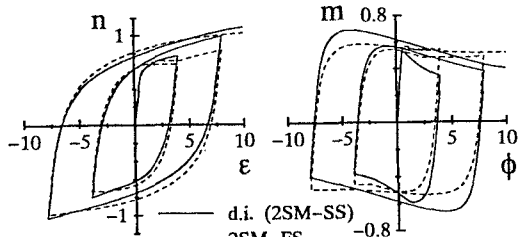


Fig. 7 Comparison between the direct integration method with the 2SM-FS (box section, $B = H = 125\text{mm}$, $t_f = 8.7\text{mm}$, $t_w = 6.1\text{mm}$, SS400)

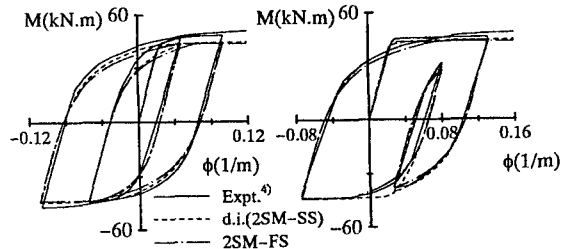


Fig. 8 Comparison with experiments ($H125 \times 125 \times 6.5 \times 9$, SS400)

CONCLUSIONS: This paper was concerned with the cyclic inelastic sectional behavior of steel members using 2SM-FS. The procedure for determining the model parameters were described and the values of the parameters for I and box sections were given. Finally, the accuracy of the 2SM-FS was verified by comparing the obtained results with experiments.

REFERENCES: [1] Suzuki, T., Mamaghani, I.H.P., Mizuno, E., Usami, T., "Finite displacement analysis of steel structures with two-surface plasticity model in stress resultant space." *Proc. of the 50th Annual Meeting, JSCE*, Vol.1(A), 110-111, 1995. [2] Mizuno, E., Mamaghani, Iraj H.P., and Usami, T., "Cyclic large displacement analysis steel structures with two-surface model in force space". *ICASS'96*, Vol. 1, pp. 183-188, 1996. [3] Shen, C., Mamaghani, I.H.P., Mizuno, E., and Usami, T., "cyclic behavior of structural steels. II: Theory." *J. Engrg. Mech., ASCE*, Vol. 121(11), pp.1165-1172, 1995. [4] Minagawa, M., Nishiwaki, T. and Masuda, N., "Prediction of hysteresis moment-curvature relations of steel beams", *J. of Structural Engineering, JSCE*, Vol. 34A, pp.111-120, 1988.