## III - 398 MODELING ISOTROPICALLY CONSOLIDATED NATURAL

## SILT-SAND IN TC

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INTRODUCTION. For any rational analysis, for example by FEM, the formulated pre-peak and post-peak stress-strain relationships of the soil including the peak strength properties are necessary. For this purpose Tatsuoka and Shibuya (1992) has proposed a Generalized Hyperbolic Equation to model the stress- strain relationships of sands. Herein presented is the modified method and the results of modeling the stress-strain relationship obtained from Consolidated drained triaxial compression (CDTC) tests performed under different testing conditions.

GENERAL HYPERBOLIC EQUATION (GHE). This method is able to model a given stress-strain relation from say

0.0001% to that at the peak stress state (1-10%). On the other hand the Conventional Hyperbolic Equation (CHE) can't fit the entire stress-strain relationship for a wide range of strain. Clear explanation and definition of GHE and its constants determination are given in Tatsuoka and Shibuya (1992).

## MODELING THE STRESS-STRAIN RELATIONSHIPS OF NATURAL SILT-SAND. The stress-

strain relations in TC at a constant  $\sigma_3$  for any soil is represented by the following hyperbolic function.

$$q/q_{max} = \frac{\varepsilon_a}{\frac{q_{max}}{C_1 E_{max}} + \frac{\varepsilon_a}{C_2}}$$

Where q is the deviator stress,  $q_{max}$  is the maximum deviator stress,  $\varepsilon_a$  is axial strain,  $E_{max}$  is the maximum Young's modulus,  $C_1$  and  $C_2$  are a function of strain level (eq. (1) and (2)).

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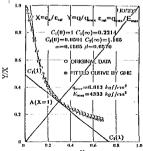
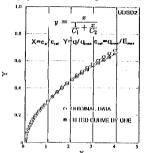


Fig. 1(b) Normalized plot using GHE.



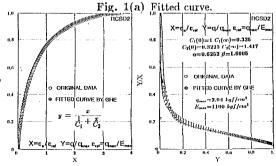


Fig. 2 Fitted curve.

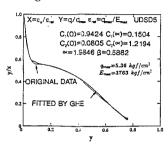


Fig. 3 Normalized plot using modified method.

$$C_1(x) = \frac{C_1(0) + C_1(\infty)}{2} + \frac{C_1(0) - C_1(\infty)}{2} cos\left(\frac{\pi}{\frac{\alpha}{x} + 1}\right)$$
 (1)

$$C_2(x) = \frac{C_2(0) + C_2(\infty)}{2} + \frac{C_2(0) - C_2(\infty)}{2} cos\left(\frac{\pi}{2 + 1}\right)$$
 (2)

The parameter  $\alpha$  and  $\beta$  can be obtained by the coordinates X=1 and Y at point A (Fig. 1(b)) and the values of  $C_1(1)$  and  $C_2(1)$  in to eq. (1) and (2). The values of  $C_1(1)$  and  $C_2(1)$  are the coordinates where the line tangent to the data curve at point A intersects the axes Y/X and Y. Arbitrarily chosen experimental data of test UDSD2 (Undisturbed sand), UDSD5 (Undisturbed silt-sand) and RCSD2 (Reconstitute sand) were fit by using GHE (Fig. 1 and 2).

Due to a large kink in the normalized plot (as shown in Fig. 3) the GHE could not model satisfactorily of the original data of UDSD5 (undisturbed silt-sand). To alleviate this problem the following approaches were taken for determining the constants in the normalized plot of GHE. The determination of constants  $C_1$  (0),  $C_1$  ( $\infty$ ),  $C_2$  (0) and  $C_2$  ( $\infty$ ) were the same as mentioned by Tatsuoka and Shibuya (1992). To determine the constants,  $C_1$  (1) and  $C_2$  (1) the following steps were introduced.

1. Intersection point 'A'  $(X_1,Y_1)$  between the lines 'uv' and 'rs' is obtained:

$$x_{1} = \frac{C_{2}(\infty)C_{2}(0)[C_{1}(0) - C_{1}(\infty)]}{C_{2}(\infty)C_{1}(0) - C_{2}(0)C_{1}(\infty)}$$

$$y_{1} = \frac{C_{1}(\infty)C_{1}(0)[C_{2}(\infty) - C_{2}(0)]}{C_{1}(\infty)C_{2}(0) - C_{1}(0)C_{1}(\infty)}$$
(3)

The line 'pq' which is passing through 'A' is obtained:

$$y = -m_p x + (y_1 + m_p x_1)$$
 (4)  
 $m_p = \tan(\frac{\theta_1 + \theta_2}{2})$ 

Slopes  $\theta_1$  and  $\theta_2$  can be defined by,

$$tan\theta_1 = \frac{C_1(0)}{C_2(0)}$$
$$tan\theta_2 = \frac{C_1(\infty)}{C_2(\infty)}$$

3. Point 'B'  $(X_2,Y_2)$  in the normalized data with minimum distance from 'A' is de-

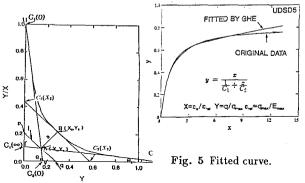


Fig. 4 Parameters determination for hyperbolic relation by modified method.

termine (Fig. 4). The distance or relative non-linearity index 'a' is given by:

$$x_2 = x_1 + a\cos(m_p)$$
  
 $y_2 = y_1 + a\sin(m_p)$  (5)

4. Determine a line which is passing through 'B' and parallel with the line 'pq':

$$y = m_p x + (y_1 - m_p x_1) + a(\sin(m_p) - \cos(m_p))$$

5. The intersections of this line with the axes give the  $C_p$  and  $C_q$ . From Eq. (4), we obtained:

$$C_p = y_1 + m_p x_1$$

$$C_q = \frac{y_1 + m_p x_1}{m_p}$$

$$C_1(X_2) = C_1(p) + a \sec(m_p)$$
  

$$C_2(X_2) = C_2(q) + a \csc(m_p)$$

 $\alpha$  and  $\beta$  can be determine by substituting,  $X_2$  and  $C_1$  ( $X_2$ ) and  $C_2$  ( $X_2$ ) into eq. (1) and (2). After this modification it is observable that 'a' becomes a significant parameter. Fig.5 shows the fitted curve using GHE with the modified constants.

CONCLUSION. After the modification a reasonable agreement between experimental data and prediction was obtained in the case where the non-linearity of stress-strain is peculiar characteristics.