Behavior of Reinforced Concrete Core Wall-Perimeter Steel Frame Hybrid Structure under Dynamic and Static Analysis

Wei LI 1 • Akihiko KAWANO 2 • Kenji SAKINO 3 • Hiroyuki NAKAHARA 4

1Member, Doctor Candidate, Department of Architecture, Graduate School of Human-Environment Studies, Kyushu University (〒10-6-1 Hakozaki, Higashi-ku, Fukuoka, 812-8581, Japan)
E-mail: li_06g@arch.kyushu-u.ac.jp

2Member, Professor, Department of Architecture and Urban Design, Faculty of Human-Environment Studies, Kyushu University (〒10-6-1 Hakozaki, Higashi-ku, Fukuoka, 812-8581, Japan)
E-mail: kawano@arch.kyushu-u.ac.jp

3Member, Professor, Department of Architecture and Urban Design, Faculty of Human-Environment Studies, Kyushu University (〒10-6-1 Hakozaki, Higashi-ku, Fukuoka, 812-8581, Japan)
E-mail: sakino@arch.kyushu-u.ac.jp

4Member, Associate Professor, Department of Architecture and Urban Design, Faculty of Human-Environment Studies, Kyushu University (〒10-6-1 Hakozaki, Higashi-ku, Fukuoka, 812-8581, Japan)
E-mail: nakahara@arch.kyushu-u.ac.jp

We have studied the behavior of Hybrid Structure with reinforced concrete core wall-perimeter steel frame under dynamic and static loads with incremental dynamic analysis (IDA) and static pushover analysis. Three different storey models, 12-storey, 20-storey and 30-storey with fishbone-shaped frame and diagonally-braced frame have been analyzed. Twenty seismic ground motion records (FEMA) are used to obtain an average response optimally in IDA. We have compared the storey shear force between IDA (ten different intensities, PGV from 10kine to 100kine) and static pushover analysis to estimate more thoroughly structural performance with plastic development; additionally, we have discussed the interstorey shear force amplificatory ratio $\gamma$ between IDA and static pushover analysis, found it’s quite related to the input intensity and location along the building. Finally we have discussed the ratio $\alpha$ to obtain the change rule about the ratio $\gamma$ of frame and wall towards the ratio $\gamma$ of total storey.

Key Words: RC Core Wall, Steel Frame, Hybrid Structure, Incremental Dynamics Analysis, Pushover

1. Introduction

According to the general knowledge, a hybrid structure means that the structures are combined by at least two component parts of different materials. The combination is supposed to obtain the excellent performance after mixing two or more kinds of structure systems reasonably which simplex structure system doesn’t have.

The hybrid structure is mostly applied to high-rise and extremely high-rise buildings. It varies in forms and names for the combination of materials, cross sections and structure forms. There are three kinds of hybrid structures in common use 1).

The first is Concrete-Filled Steel Tubes Column Systems (CFTs). CFTs offer a number of advantages when used in seismic-resistant frames. The concrete infill confined by the steel tubes provides increased axial stiffness and load capacity. The concrete fill also restrains local buckling of the tube, and increases member ductility, while permitting more slender steel elements.

The second is Reinforced Concrete/Steel Reinforced Concrete Column Systems (RCs/SRCs). The RCs systems are moment frames consisting of RC columns and steel beams. They provide excellent stiffness with RC columns and energy dissipation capacity through steel beams. As opposed to conventional steel or RC moment frames, the problems associated with connections are greatly reduced, and the RCs frames are generally more economical than the purely steel or RC moment frames.

The third is Reinforced Concrete/Steel Reinforced Concrete Hybrid Wall Systems. Hybrid wall systems consist of RC or SRC walls to provide resistance against lateral forces and steel-beam and column-frame systems to support the gravity loads. Most of the lateral strength and stiffness to the system is provided by the walls. The floor system, in addition to supporting the gravity loads, also serves to transfer the lateral forces to the walls.

The focus of this paper is on the third one. This efficient hybrid structure system is obtained when reinforced concrete core walls are used in conjunction with steel perimeter frames. For low-to-moderate-rise buildings, up to 25 to 30 stories, the core can be used to provide a majority of the lateral force resistance for earthquake and wind. For taller buildings, the use of dual systems is more common, where the perimeter frames are engaged with the core. The hybrid structure system has large lateral stiffness in each direction, the perimeter frames mainly...
support vertical loads and some part of horizontal loads
which are distributed based on the lateral stiffness of dual
systems. The lateral stiffness of reinforced concrete core
wall accounts for more proportion of the total stiffness,
thus the core walls resist more horizontal loads. Specially
according to yield strength of sub-structure, the yield
strength of reinforced concrete core walls is much smaller
than that of perimeter frames, so the core walls have
relatively redundant stiffness but insufficient strength
which reduce its anti-earthquake performance. The
plastic hinges of the hybrid structure appear in the core
walls under severe earthquake, and this kind of plastic
hinge mechanism is very harmful to the structure system.
With excessive deformation and damage in the core
walls, the whole structure or its sub-structure would lose
stabilization and collapse. The successful performance of
such hybrid structural systems depends on the adequacy
of the primary individual components which are the core
walls, steel frames, and frame-core connections 3). In this
paper, the authors mainly think about finding the rule of
the storey shear force distribution in different proportion
of core walls and perimeter frames, and interstorey shear
force amplificatory ratio γ of different intensity between
static and dynamic analysis.

2. Incremental Dynamic Analysis
Incremental Dynamic Analysis (IDA) 3, 4) is a parametric
analysis method that has recently emerged in several
different forms to estimate more thoroughly structural
performance under seismic loads. It involves subjecting
a structural model to one (or more) ground motion
record(s), each scaled to multiple levels of intensity,
thus producing one (or more) curve(s) of response
parameterized versus intensity level.

The growth in computer processing power has made
possible a continuous drive towards increasingly accurate
but at the same time more complex analysis methods.
Thus the state of the art has progressively moved from
elastic static analysis to dynamic elastic, nonlinear static
and finally nonlinear dynamic analysis. In the last case
the convention has been to run one to several different
records, each once, producing one to several analyses,
mostly used for checking the designed structure. On the
other hand methods like the nonlinear static pushover
(SPO) (ATC, 1996) or the capacity spectrum method
(ATC, 1996) offer, by suitable scaling of the static force
pattern, a “continuous” picture as the complete range
of structural behavior is investigated, from elasticity to
yielding and finally collapse, thus greatly facilitating our
understanding.

By analogy with passing from a single static analysis
to the incremental static pushover, one arrives at the
extension of a single time-history analysis into an
incremental one, where the seismic “loading” is scaled.
It has also been adopted by the U.S. Federal Emergency
Management Agency (FEMA) guidelines (FEMA, 2000a,
b) as the Incremental Dynamic Analysis (IDA) and
established as the state-of-the-art method to determine
global collapse capacity.

As a first step, let us define the fundamental concept of
scaling an acceleration time history that we need. Assume
we are given a single acceleration time-history, selected
from a ground motion database which will be referred
to as the base, “as-recorded” (although it may have been
pre-processed by seismologists, e.g., baseline corrected,
filtered and rotated), unscaled accelerogram α1 , a vector
with elements α1(t_i), t_i = t_1, t_2,…,t_n. To account for more
severe or milder ground motions, a simple transformation
is introduced by uniformly scaling up or down the
amplitudes by a scalar λ ∈ [0, +∞): α_λ = λ·α1. Such an
operation can also be conveniently thought of as scaling
the elastic acceleration spectrum by λ or equivalently.
Usually we use Peak Ground Velocity (PGV) to control
the input seismic intensity, by using this scaling method
we get twenty seismic earthquake records, PGV from
10kine to 100kine.

3. Analysis model and method of hybrid
structures
3.1 Analytical plan
The floor plan of a representative hybrid building using
this structure system is shown in Fig.1. The walls may be
reinforced conventionally with longitudinal and transverse
reinforcement, or may include embedded structural steel
boundary columns in addition to conventional reinforcing
bars.

For simplifying the analysis procedure, we can turn
the 3-dimention model into 2-dimention planar model
that is shown in Fig.2. The pure frame portion and the
frame with core walls portion are linked by link elements
which have large rigidity with two pin joints that can
transfer load and deformation 5). Because of the limits of
our analysis program, the problem is how to compute the
core-wall in our model. In Japan, there is a conventional
method to simulate the shear wall with the equivalent
diagonally-braced frame.

![Fig.1 Floor plan of reinforced concrete core wall-perimeter frame system](image-url)
3.2 Equivalent Method for Shear Wall

The equivalent method is mentioned in Masafumi Inoue and Masahide Tomii's paper named Method of estimation of rotational rigidity of the corner connections of framed shear walls for their equivalent diagonally-braced frames.

The cross sectional area, \( A_b \), of the braces in the equivalent frame is determined by equalizing the shear rigidity of the shear wall to that of the equivalent frame. The drift, \( \delta_{ws} \), due to shearing deformation of the shear wall is given by Eq. (1) (see Fig. 3 (a)).

\[
\delta_{ws} = \frac{k_w h}{G A_w} X = \frac{2(1+\nu)k_w h}{E A_w} X
\]  

(1)

where
\( E \): Young's modulus
\( \nu \): Poisson's ratio
\( k_w \): shape factor for shearing deformation of shear wall
\( G \): shear rigidity \([=E/(1+\nu)]\)
\( h \): story height
\( A_w \): horizontal sectional area of wall
\( X \): horizontal force

The drift, \( \delta_{bs} \), of the equivalent frame is given by Eq. (2) (see Fig. 3 (b))

\[
\delta_{bs} = \frac{1}{E A_b} \frac{(h^2 + l^2)^{1.5}}{2l^2} X
\]  

(2)

where
\( l \): distance from center to center of edge columns

The cross sectional area, \( A_c \), of each brace in the equivalent frame is given by Eq. (3) when \( \delta_{ws} \) and \( \delta_{bs} \) respectively given by Eqs. (1) and (2) are made equal.

\[
A_b = \frac{G}{E} \frac{t}{l} \frac{(h^2 + t^2)^{1.5}}{2k_w lh}
\]  

(3)

where
\( t \): thickness of wall

The cross sectional area, \( A_{bc} \), of columns in the equivalent frame is determined by equalizing the flexural rigidity, \( EI_w \), of the horizontal sectional area of the shear wall to the flexural rigidity, \( EI_b \), of the equivalent frame. The \( EI_w \) is given by Eq. (4).

\[
EI_w = E \left[ 2 \left( I_{wc} + A_{wc} \frac{l^2}{2} \right) + \frac{t l^3}{12} \right]
\]  

(4)

where
\( I_{wc} \): moment of inertia of the cross sectional area of the edge columns of a shear wall
\( A_{wc} \): cross sectional area of each edge column of a shear wall
\( l' \): clear span of the boundary frame of a shear wall

The \( EI_b \) is given by Eq. (5).

\[
EI_b = 2EA_b \frac{l^2}{2}
\]  

(5)

The \( A_{bc} \) given by Eq. (6) is obtained by equalizing \( EI_w \) and \( EI_b \) respectively given by Eqs. (4) and (5).

\[
A_{bc} = \frac{4}{l^2} I_{wc} + A_{wc} + \frac{t l^3}{6l^2}
\]  

(6)

The equivalent frames of shear walls are determined by using the values of \( A_b \) and \( A_{bc} \) respectively given by Eqs. (3) and (6).

3.3 Material hysteresis property

Two types of Steel materials are used in our analysis model, SN490 is used for H shape Steel beam and reinforced bar in concrete and BCR295 for \( \square \) shape steel perimeter columns. The following figs (4, 5, 6, 7) have shown their hysteresis property and stress-strain relation.

3.4 Analytical Model

Three kinds of models were analyzed, 12-storey, 20-storey, and 30-storey which include low-rise, moderate-rise and high-rise buildings in practical use. The analytical model is shown in Fig.8 and 9 with fishbone-shaped frame model which can easily display the behavior of frame and represent prevalent structure characteristic in different forms, and reduce the analysis time 7; the numbers on the top are the mass for each storey. The average mass is 1.0ton/m², the story height is 3.6m except 4.0m at the first story, the region coefficient equals to 1.0, the standard base shear coefficient equals to 0.2 at first level and 1.0 at second level. The static pushover load distribution equals to Ai distribution according to the Japanese code (Fig.8 a) 8. The seismic waves of the ground motion records for the incremental dynamic time-history analysis are
LA1-LA20 (FEMA). Newmark β method is used in the dynamic analysis, the damping factor of the first and the second mode shape equals to 0.03, the factor β equals to 0.25. The PGV of the seismic waves from LA01 to LA20 is equal to 10, 20, 30, 40, 50, 60, 70, 80, 90, 100kine.

The fishbone-shaped frame part has 4 different stiffness, the first one is basic, the others are 2, 3, and 6 times stiffness to the basic one. On account of the limited space of the paper, only basic one and 6 times models results are showed here to express the influence of stiffness between frame and wall parts.

4. Analytical results and discussion

4.1 Comparison Rule

When we compare the difference of the responses of the structure between dynamic analysis and static pushover analysis, the key question is how to compare, we should make a rule to compare the result. So we define a rule as follows,

1. Find the center of the Ai distribution Load (Get the storey number as shown in Fig. 8),
2. Find the maximum deformation of this storey under the Dynamic Time-History analysis,
3. Find the step of the static pushover analysis that the deformation of this storey probably equals to the deformation we find in step 2.

From the rule, we get the state that is able to be discussed as shown in Fig.10. The thin dash line means the result for each seismic wave under Time-History Analysis, the wide line means the average of the result, and the wide dash line means the result for static pushover analysis, we can see that the profile deformation in different analysis perfectly match. So in this state, we can discuss the storey-drift angle, shear distribution, etc between dynamic and static analysis.

4.2 Results and Discussion

Our analytical models are three kinds of different height hybrid structures including perimeter steel frame and reinforced concrete core wall, each of them has its own property and deformation pattern. For example, pure frame has a shear deformation pattern and reinforced concrete core wall has a bending deformation pattern, especially the core wall has a large stiffness but a very smaller deformation than pure frame, when shear wall begin to crack, the frame is still elastic, when frame begin to yield, the shear wall almost reach its ultimate status.

The behavior of this kind of hybrid structure is very complex, only static pushover analysis can't describe its behavior clearly, so dynamic analysis is needed. We modify the PGV equal to 10kine, 20kine, 30kine, 40kine, 50kine, 60kine, 70kine, 80kine, 90kine, and 100kine for each earthquake waves to change the intensity of the input ground motion, just like a dynamic pushover analysis. So we can think about the behavior of the hybrid structure in different deformation status.

Fig. 11 is interstorey shear force for only one storey under pushover static analysis and incremental dynamic analysis(IDA). For each storey, it clearly shows the difference and the relationship between two kinds of analysis with enhancing intensity. It gives the essential descriptions of the capacity ability of the buildings.
from elastic to plastic status, while the seismic intensity changing from 10kine to 100kine, the difference becomes larger because of the plastic development in the structure, this phenomena has a complex relationship with plastic character of building and character of seismic records. Though the growth in computer processing has made possible to run a large number of dynamic analysis, but it still need much time to get the result especially the building more higher and more complex now. It tells us one can easily understand the behavior of the hybrid structure under seismic dynamic loads from the results of the static pushover analysis.

To investigate the whole building’s behavior, an amplificatory ratio \( \gamma \) was defined which equals to dynamic shear force divide static shear force \( \gamma = \frac{Q_D}{Q_S} \).

Figs. 12, 13 and 14 show the ratio \( \gamma \) for each storey of three different height model under enhancing intensity with basic stiffness fishbone-shaped frame. In the legends, C-Ratio, W-Ratio and S-Ratio mean ratio \( \gamma_F \), \( \gamma_W \), and \( \gamma_S \) respectively which will be explained next. One can see the behaviors of frame columns and core shear walls are quite different. Because the deformation pattern between frame and wall is different, frames have shear deformation pattern, walls have flexure deformation pattern, the deformation pattern of the whole building have both of these two deformation character, so the behavior of frames and walls is quite different under dynamic and static analysis, the variety of the ratio \( \gamma \) of frames is smoother than that of walls, the ratio \( \gamma \) of walls is more sensitive, especially shear walls are the main part of the building to provide resistance against lateral forces, most of the lateral strength and stiffness is provided by walls, it’s so important to understand the behavior of the building under seismic dynamic loads. While the input intensity becomes higher, the ratio \( \gamma \) of the whole storey becomes larger in three different height models because of the plastic development in the model which prominently affect the behavior under seismic dynamic loads. In basic model, \( \gamma_S \) of 12 storey changes from 1.05 to 1.15, \( \gamma_S \) of 20 and 30 storey changes from 1.3 to 1.5 with enhancing intensity; In 6 times model, \( \gamma_S \) of 12 storey changes very small, \( \gamma_S \) of 20 and 30 storey changes from 1.05 to 1.2 with enhancing intensity; while the stiffness of fishbone-shaped frame enhancing, ratio \( \gamma_S \) has tendency to change smaller.

Usually we care the relationship of the interstorey shear force of the frame and wall with the interstorey shear force of the storey, so we standardize these figs. The definition is given by Eq. (7) and (8):

\[
\alpha_F = \frac{\gamma_F}{\gamma_S} \quad (7)
\]

\[
\alpha_W = \frac{\gamma_W}{\gamma_S} \quad (8)
\]
Fig. 12 The amplificatory ratio $\gamma$ of different intensity 12S
Basic stiffness model

Fig. 13 The amplificatory ratio $\gamma$ of different intensity 20S
Basic stiffness model

Fig. 14 The amplificatory ratio $\gamma$ of different intensity 30S
Basic stiffness model

Fig. 15 The amplificatory ratio $\gamma$ of different intensity 12S
6 Times stiffness model

Fig. 16 The amplificatory ratio $\gamma$ of different intensity 20S
6 Times stiffness model

Fig. 17 The amplificatory ratio $\gamma$ of different intensity 30S
6 Times stiffness model
Fig. 18 The ratio $\alpha$ of different intensity 12S Basic stiffness model

Fig. 19 The ratio $\alpha$ of different intensity 20S Basic stiffness model

Fig. 20 The ratio $\alpha$ of different intensity 20S Basic stiffness model

Fig. 21 The ratio $\alpha$ of different intensity 12S 6 Times stiffness model

Fig. 22 The ratio $\alpha$ of different intensity 20S 6 Times stiffness model

Fig. 23 The ratio $\alpha$ of different intensity 20S 6 Times stiffness model
where
\[ \gamma_F : \text{the amplificatory ratio of frame} \]
\[ \gamma_W : \text{the amplificatory ratio of wall} \]
\[ \gamma_S : \text{the amplificatory ratio of storey} \]

By using Eq. (7) and (8), we get the figs. 18, 19 and 20 for basic stiffness models; figs. 21, 22 and 23 for 6 times stiffness modes. In the legends, the symbols C/S means ratio \( \gamma_F \), W/S means ratio \( \gamma_W \). The change rule of three different height models is very similar; the ratio \( \alpha_F \) of the frame changes smaller, the ratio \( \alpha_W \) of the wall changes larger, but it’s not prominent. Below the two thirds of the height of the model, the ratio \( \alpha_F \) and \( \alpha_W \) almost don’t changes. Upon the two thirds of the model especially the top three storeies, the ratio \( \alpha_W \) of wall is very large, there are two reasons to explain this phenomena, the first is whipping effect of the model under seismic dynamic load, and the second is that the deformation pattern between frame and wall is different, frames have shear deformation pattern, walls have flexure deformation pattern, especially at the top storeys of the building. while the model is higher, the effect is more obvious. While the stiffness of fishboned-shaped frame enhancing, the frame stiffness take more proportion of whole storey, so \( \alpha_F \) becomes closer to \( \alpha_S \), on the contrary \( \alpha_W \) becomes more far to \( \alpha_S \). Through the ratio \( \gamma \), \( \alpha_F \) and \( \alpha_W \), one can clearly understand and describe the behavior of the frame and wall separately under dynamic and static analysis.

5. Conclusive remarks

From the analytical results above paragraphs, we can get some valuable points of view to supervise the real practical design method as follows,
1. Incremental Dynamic Analysis (IDA) is a useful parametric analysis method to estimate more thoroughly structural performance under seismic loads; and it can be adopted to determine global collapse capacity of the building.
2. The rule to compare static and dynamic analysis defined is viable, it can be adopted in any different height buildings.
3. The result of nonlinear plastic time-history dynamic analysis is based upon the character of the seismic record we select; it's sensitive for each seismic record. Basically it's impossible to compare the result between dynamic and static pushover analysis through only one or several seismic records. One should select large numbers of records to reduce the affection of certain specific record in the statistical sense.
4. Through the pushover and IDA curve for each storey, one can easily understand the behavior of the hybrid structure under seismic dynamic loads from the results of the static pushover analysis quickly.
5. The interstorey shear force tends to become larger under seismic dynamic loads than static pushover analysis, also it is related to input intensity of seismic records. The amplificatory ratio \( \gamma \) of frame, wall and storey is different in each storey, the change rule is similar in three different height models. Through the ratio \( \gamma \), \( \alpha_F \) and \( \alpha_W \) one can compare the interstorey shear force of frame, wall and storey under dynamic and static analysis separately.
6. when one calculates amplificatory ratio of dynamic analysis for design, one should take into account the wall ratio, in other words, the stiffness distribution between wall and frame should be taken into account.

Acknowledgments

This research is a part of the international cooperative program of China-Japan research on seismic performance of hybrid structures of steel-concrete in the high seismic intensity region. Many investigators are involved in this program. A large number of numerical analysis will be done on the Japanese side by the nonlinear finite element analysis program of Prof. Kawano, and some large-scale experiments will be done on the Chinese side by Xi’an Architecture Technology University, they will analyses the hybrid structure system by Ansys too.

References