

# SEISMIC RISK ANALYSIS BASED ON STRAIN ENERGY ACCUMULATION IN FOCAL REGION

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The object of this paper is to propose a stochastic method for evaluating the magnitude of future earthquakes taking account of the nonstationariness in earthquake occurrence. For this purpose, the strain energy accumulation in a focal region was estimated by means of earthquake data of the past 100 years in Japan. Furthermore, distributions of maximum ground acceleration were derived by means of the attenuation law. As a result, we found that the distributions of maximum ground acceleration fit type III extreme value distributions and that the expected values of those distributions depend on the strain energy accumulation significantly. Finally, it is pointed out that the nonstationariness in earthquake occurrence should be taken into consideration in order to evaluate the earthquake load in design.

*Keywords*: earthquake, nonstationariness, strain energy accumulation in focal region, magnitude, maximum ground acceleration, extreme value distribution

## 1. INTRODUCTION

Since Japan is located on the subduction zone of a few plates, seismicity is active and many structures have been damaged during large earthquakes. So, in case of evaluating the characteristics of earthquake load in design, it is very important to develop a method characterized by a high degree of accuracy to estimate the ground motion within the service life of a structure.

In estimating the ground motion, there are deterministic and probabilistic methods. The former methods estimate the ground motion by means of the dislocation model. Suzuki and Satou<sup>1)</sup> have applied this model to a great earthquake expected in the Tokai region. The latter methods evaluate the probability distribution or the expected value of recurrence of the ground motion by considering earthquake occurrence as a probabilistic event. Kawasumi<sup>2)</sup> has proposed one such method employing cumulative frequencies. At present, it can be pointed out that probabilistic methods are more suitable for estimating the ground motion than deterministic methods, because a geophysical model and its parameters in earthquake occurrence are not accurately known<sup>3)</sup>.

However, in traditional probabilistic methods, it is assumed that the process of earthquake occurrence is temporarily stationary, i.e., that the

probability of occurrence is invariant in time. Actually, it is rare for another large earthquake to occur in the same region immediately after a large earthquake. Moreover, since the service life of a structure ranges from several decades to about 100 years, it is not reasonable to assume stationariness in earthquake occurrence within the service life of a structure.

The object of this paper is to estimate strain energy accumulation in focal regions at present and to propose a new method for evaluating the ground motion which may inflict damage on structures in the future.

## 2. STATE OF THE ARTS AND THERE QUESTIONS

Some seismic risk analyses in which the nonstationariness in earthquake occurrence is taken into consideration have been suggested. Typical models of seismic risk analyses—the time-predictable model, the slip-predictable model and the semi-Markov model—are reviewed as follows.

### (1) Time-predictable model

This model was proposed by Shimazaki et al.<sup>4)</sup> Time history of the stress accumulation and release in a fault is represented schematically in Fig.1. That is, stress accumulates at a constant rate up to a certain threshold, at which time an earthquake occurs and accumulated stress is released. The size of the earthquake is determined by the level of the released stress. The time when the next earthquake will occur is predictable given the size of the preceding earthquake, but it is difficult to estimate the size of the next earthquake. Anagnos et al.<sup>5)</sup> described this model by following Markov's renewal process.

$$P\{Y_{n+1}=J, T_{n+1}-T_n \leq t | Y_0, \dots, Y_n; T_0, \dots, T_n\}$$

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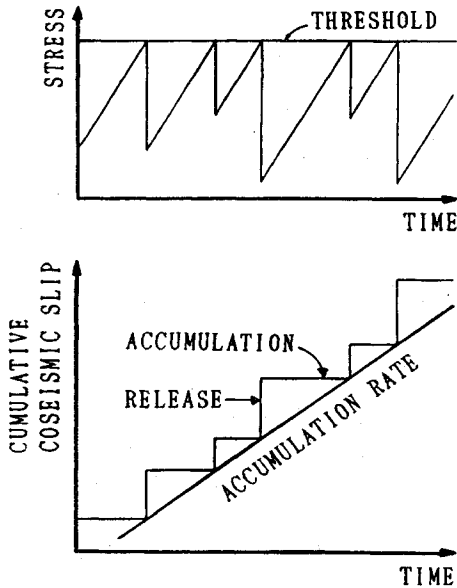


Fig.1 Time-predictable model

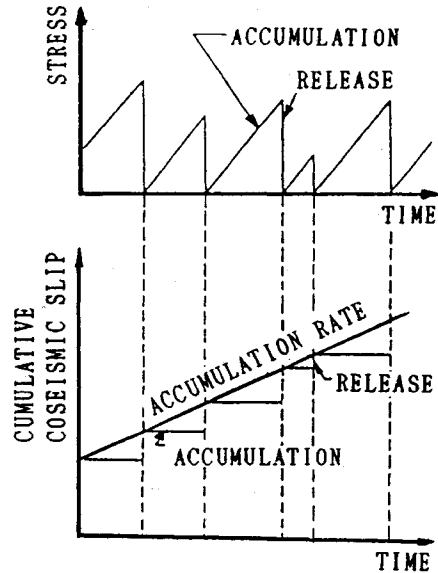


Fig.2 Slip-predictable model

$$= P[Y_{n+1}=J, T_{n+1}-T_n \leq t | Y_n=I] \dots\dots\dots (1)$$

where I, J = the state depending on the size of the earthquake,  $Y_n$  = the state of the fault after the nth event and  $T_n$  = the time of the nth event.

This means that the joint probability from present state to the next state depends only on the present state and is independent of past history. A change of stress release by measuring a coseismic slip in a fault has been proposed, because it is difficult to directly measure the level of stress release.

(2) Slip-predictable model

This model, proposed by Shimazaki et al.<sup>4)</sup>, is a method that predicts the size of an earthquake based on the interval times. Fig.2 shows schematically the stress accumulation and release at a fault. For this model, it is assumed that the stress at the fault drops to zero after each earthquake. So, the time up to the next event is random, and the longer the interval, the greater the event due to the release of the larger stress. Kiremidjian et al.<sup>6)</sup> extend the slip-predictable model to a site hazard model using the attenuation law. However, the occurrences of successive earthquakes are independent according to the above assumption, and the process of foreshock, mainshock and aftershock at the same fault cannot be rationally explained.

(3) Semi-Markov model

This model proposed by Patwardhan et al.<sup>7)</sup> on the basis of the assumption that the size of the earthquake and the interval of time until the next earthquake is influenced by the amount of strain

energy released by the previous earthquake. However, a weakness of this model is that subjective assessment is required when classifying the magnitude. That is, the evaluated value is supposed to vary with the classified magnitude because if the magnitude is changed by only 1.0, the released energy varies by about thirty times. Also, the validity of the assumed probability distribution for the time interval is questionable.

As mentioned above, it is necessary to harmonize the stochastic model with the geophysical model of earthquake occurrence for purposes of seismic risk analysis, because the parameters in any model contain some uncertainties. Therefore, we based our research on the theory of plate tectonics<sup>8)</sup>. This theory postulates that "the strain energy is accumulated due to the interaction movement of the plates. At the time when the accumulated strain energy reaches a certain extent, an earthquake occurs due to the break of the plates, and the strain energy is released. So, some interval is necessary for the accumulation of strain energy leading to the occurrence of the next event."

In this analysis, it is assumed that the size and the time interval before the occurrence of the next earthquake depend on the strain energy accumulation in the plate at present. A method for forecasting the magnitude of future earthquakes and the distributions of maximum ground acceleration at several main cities in Japan is proposed.

3. SEISMIC RISK ANALYSIS

In this analysis, a focal region which would

influence Japan is restricted to latitudes from 25°N to 50°N and longitudes from 125°E to 150°E. This zone is divided by meshes of 0.5° and relative strain energy accumulation in each mesh at present are estimated. Next, in each mesh, the extremal distributions of magnitude of earthquakes which are expected to occur in the next n years are estimated. Furthermore, the extremal distributions of maximum ground acceleration at main cities are derived by means of the attenuation law.

Presently, it is difficult to estimate the absolute strain energy accumulation, but seismic risk analysis can be performed by estimating the relative strain energy accumulation, according to the following assumptions.

**(1) Earthquake data**

In this analysis, we employ data on earthquakes occurring in or near Japan from 1885 to March 1988 available from the Meteorological Agency<sup>9)-13)</sup>. However, since the accuracy of methods used in the past to evaluate magnitude is unreliable, the data are corrected by means of the following method<sup>14)</sup> proposed by the Ministry of Construction. The method is based on the assumption that “the long-term incline of the curved line of energy accumulation is almost constant and that the incline from 1926 to 1973 shows a value peculiar to Japan.” The magnitudes of earthquakes which occurred from 1885 to 1925 are corrected by the following formulas.

$$\begin{aligned} 1885-1895 &: M=M'-0.5 \\ 1896-1915 &: M=M'-0.6 \dots\dots\dots (2) \\ 1916-1925 &: M=M'-0.5 \\ 1926- &: M=M' \end{aligned}$$

where M=magnitude before correction and M'=magnitude after correction.

We consider that a deep earthquake does not have much influence on surface ground motion, that it is different from an earthquake with a focal depth within 100 km in focal mechanism and that plate thickness is approximately 100 km. Therefore, we limited our investigation to earthquakes with a focal depth of 100 km or less occurring after 1926 when focal depth was added to earthquake data.

**(2) Fault model**

In general, fault movement is not uniform in either time or space. But fault movement must be simplified for the sake of modeling the earthquake occurrence from a technical viewpoint. So in this analysis, it is assumed that a rectangular fault occurs at the time of earthquake occurrence. Here, its center agrees with the epicenter, the ratio of its long side to its short side is 2 : 1, and a section of the fault is at an angle of 45° with the horizontal plane. Moreover, it is assumed that the long side

runs parallel to a longitudinal line if the epicenter is located at latitudes from 35°N to 41°N, and parallel to a latitudinal line if not<sup>15)</sup>.

Furthermore, it is supposed that strain energy is released uniformly, according to the concept of the basic fault model by Kanamori<sup>16)</sup> in proportion to some meshed part of the shadow which the rectangular fault casts on the horizontal plane. In practice, however, the areas releasing the strain energy do not always spread around the epicenter, but stretch in only one direction in many cases. Therefore, with regard to data on such faults included in the earthquake fault parameter handbook in Japan<sup>15)</sup> and to enable interpretation of the shapes of the faults, it is assumed that the epicenter agrees with the center of the faults. Concerning the relation between section of a fault and magnitude, the proposed equation by Satou<sup>15)</sup> is adopted, and the length of the long side of a fault is determined by the following equation.

$$\log L = 0.5M - 1.88 \dots\dots\dots (3)$$

where L=length of the long side of a fault and M=magnitude.

Then, a released amount of strain energy is assumed by the following equation proposed by Gutenberg and Richter.

$$\log E = 1.5M + 11.8 \dots\dots\dots (4)$$

where E=released amount of strain energy and M=magnitude.

**(3) Cluster division of each mesh**

It is assumed that the rate of strain energy accumulation is constant regardless of time. In general, there are areas which are similar as to the changing conditions of the plates and release conditions of the strain energy. But it is difficult to accurately estimate the accumulation and the release of strain energy currently. In this analysis, therefore, in order to grasp the relative strain energy accumulation in each mesh, each mesh is classified into the following three clusters based on the standard of the distribution of the sum of total released energy in each mesh from 1885 to March 1988. This assumption is based on the thinking that it is more rational to apply the ergodicity to the meshes in which the released rate of strain energy is almost equal than to all meshes. The cluster division is determined by considering the relationship between the earthquake magnitude and the amount of earthquake data.

- 1) cluster 1 :  $M_E \leq 7.4$
- 2) cluster 2 :  $7.4 < M_E \leq 7.7 \dots\dots\dots (5)$
- 3) cluster 3 :  $M_E > 7.7$

where  $M_E$ =the magnitude into which the annual average released energy in a mesh from 1885 to

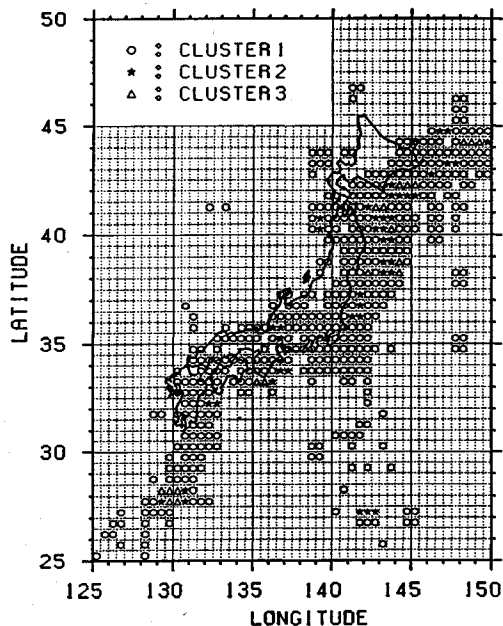


Fig.3 Cluster division of each mesh

March 1988 is converted by equation (4).

Moreover, the amount of the annual average released energy for each cluster is averaged, and it is defined as the progress rate of strain energy accumulation. Furthermore, in the case of  $M_E < 4.5$ , it is regarded as the strain energy released mainly by the inelastic slip and is not dealt with because the released strain energy is small. The result of classifying each mesh is shown in Fig.3. The meshes not indicated by marks do not belong to any cluster. From this figure, it is recognized that many earthquakes have occurred along the plates.

(4) Evaluation of the strain energy accumulation in each mesh at present

In order to evaluate the relative strain energy accumulation ( $E_{ij}$ ) in a mesh ( $i, j$ ) which latitude  $i^\circ N$  and longitude  $j^\circ E$  are the center, it is necessary to estimate the strain energy accumulation of the plate at the time of occurrence of the oldest earthquake adopted in this analysis. In general, it is supposed that the recurrence period is peculiar to each focal region, but it is difficult to evaluate them strictly at present. Kanamori<sup>8)</sup> reported that the average interval time of a great earthquake with a magnitude on the order of 8.0 is about 100 years on the Pacific side and offing. So in this analysis, it is assumed that all strain energy accumulation is released at least once about every 100 years in each mesh. Based on this assumption, the minimum strain energy accumulation ( $\min E_{ij}$ ) on the strain energy-time curve is regarded as being relative strain energy accumulation 0, and the strain

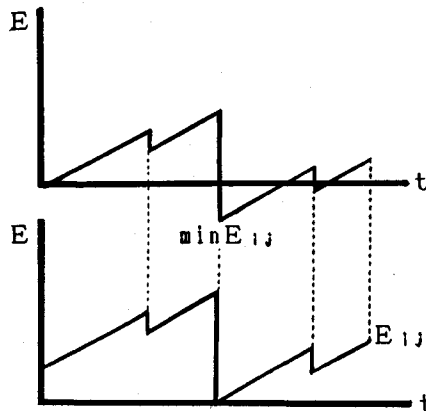


Fig.4 Parallel movement of the strain energy-time curve

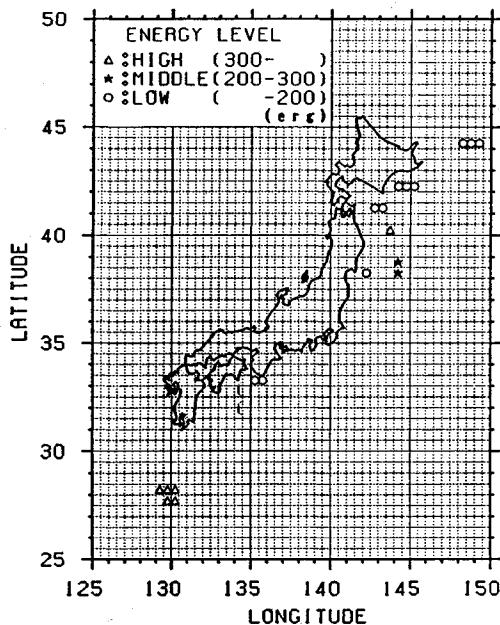


Fig.5 Strain energy accumulation (Cluster 3)

energy-time curve is moved in parallel as shown in Fig.4. The relative strain energy accumulation ( $E_{ij}$ ) in each mesh at present are estimated by the preceding method. The value of the relative strain energy accumulation in each mesh of each cluster is represented in Fig.5 to 7. In cluster 3, the relative strain energy accumulation is divided into three classes, i. e., high (more than 300 erg), middle (200-300 erg) and low (less than 200 erg). In cluster 2, the accumulation is divided into high (more than 150 erg), middle (100-150 erg) and low (less than 100 erg). As the strain energy accumulation in all meshes of cluster 1 are not high, that cluster is divided into three equal parts.

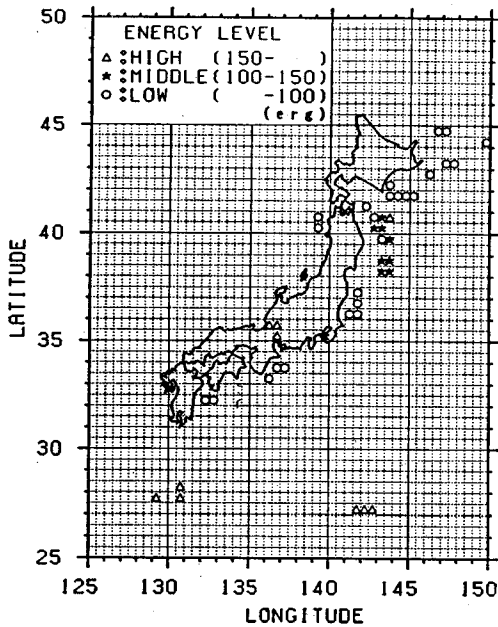


Fig.6 Strain energy accumulation (Cluster 2)

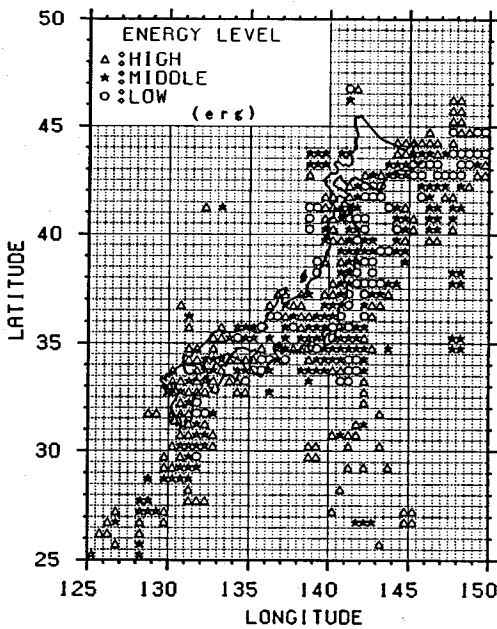


Fig.7 Strain energy accumulation (Cluster 1)

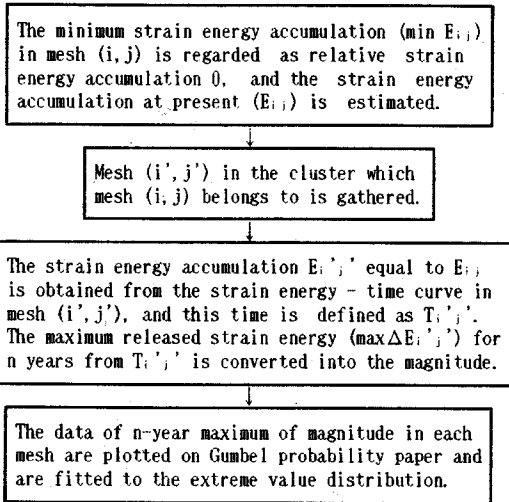


Fig.8 Flow-chart of the analysis

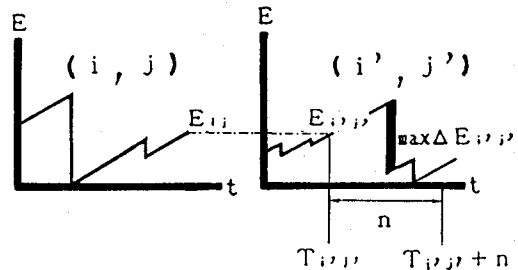


Fig.9 Schematic figure of the analysis

(5) Evaluation of extremal distribution of magnitude considering the strain energy accumulation at present

In this section, the extremal distributions of the magnitude in each mesh are evaluated. The process by which the strain energy is released corresponding to the size of the earthquake, and is again accumulated as time passes, is repeated in each

zone. Thus, the strain energy accumulation at present greatly influences the extremal distribution of magnitude of the earthquake expected to occur in the future. If sufficient earthquake data are gathered, it is possible to obtain the extremal distributions of magnitude of each mesh. However, the earthquake data measured by seismograph in Japan are 100 years old at most ; this period of observation is not sufficient in light of the recurrence period of great earthquakes. So in this analysis, to evaluate the extremal distributions of magnitude in each mesh, the ergodicity is applied to each mesh in the same cluster. Fig.8 shows a flow-chart of the analysis based on this assumption. Fig.9 shows this method schematically. First, the strain energy accumulation of  $E_{ij}$  in a mesh (i,j) at present is evaluated, and the strain energy accumulation of  $E_{ij'}$  equal to  $E_{ij}$  is determined based on strain energy-time curves in other meshes of the same cluster. Next, this time is defined as  $T_{ij'}$  and the maximum released strain energy ( $\max \Delta E_{ij'}$ ) for n years from  $T_{ij'}$  is converted into the magnitude by equation (4). Some samples from each mesh (i,j) are obtained.

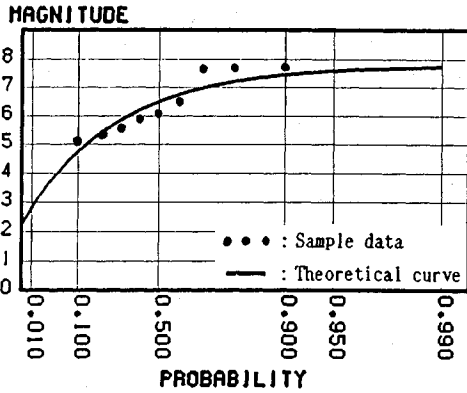


Fig.10 Distribution of 50-year maximum of magnitude (Cluster 3)

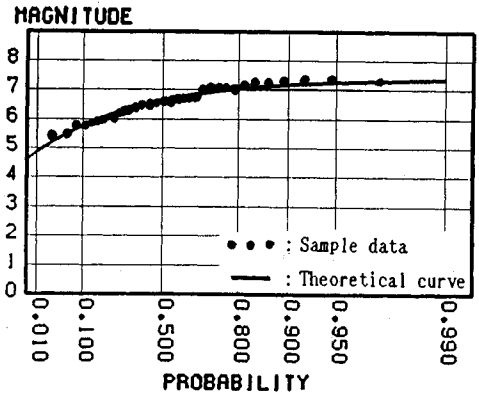


Fig.11 Distribution of 50-year maximum of magnitude (Cluster 2, Energy level=Middle)

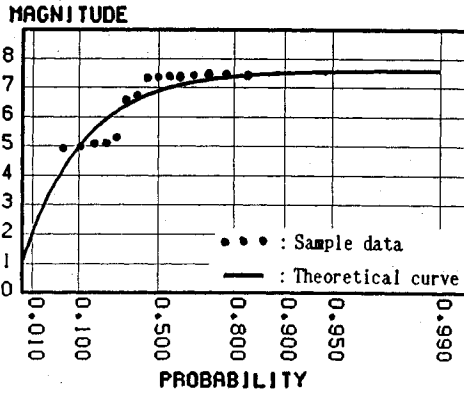


Fig.12 Distribution of 50-year maximum of magnitude (Cluster 2, Energy level=High)

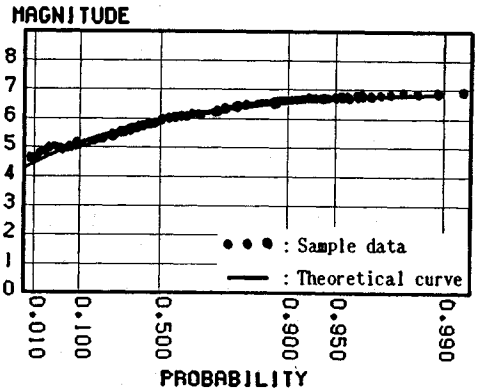


Fig.13 Distribution of 50-year maximum of magnitude (Cluster 1)

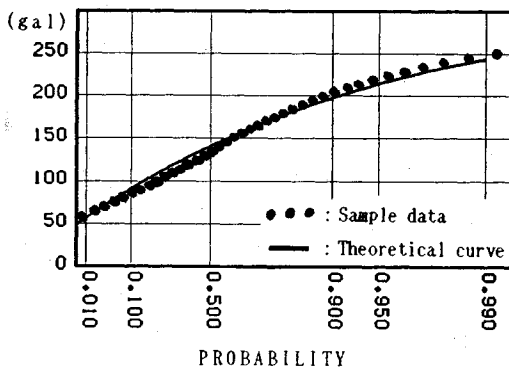


Fig.14 Distribution of 50-year maximum of maximum ground acceleration at Sendai

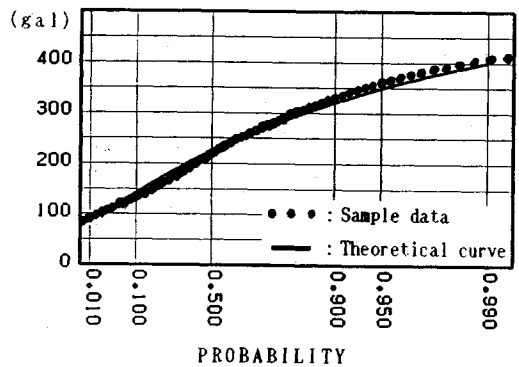


Fig.15 Distribution of 50-year maximum of maximum ground acceleration at Tokyo

To evaluate the form of the distribution, these samples are plotted on Gumbel probability paper.

Assuming that  $n = 50$  years, the samples in meshes around Sendai are plotted on Gumbel probability paper in Fig.10 to 13. Fig.10 shows the extremal distribution of cluster 3, Fig.11 and 12

show that of cluster 2 and Fig.13 shows that of cluster 1. On Gumbel probability paper, the type I extreme value distribution is indicated by a straight line, type II is indicated by a lower convex curve and type III is indicated by an upper convex curve. The upper limit value is decided from

**Table 1** The expected values and the coefficients of variation of the extremal distributions of maximum ground acceleration at main cities

Name of City	Statistics	1 0-Year	2 0-Year	3 0-Year	4 0-Year	5 0-Year
SAPPORO	Mean Value (gal)	41	42	45	46	46
	C O V (%)	16.2	15.9	15.6	15.4	14.6
SENDAI	Mean Value (gal)	127	129	139	140	143
	C O V (%)	28.7	28.5	28.5	28.3	28.8
TOKYO	Mean Value (gal)	189	199	211	224	229
	C O V (%)	29.1	29.9	30.0	29.9	30.0
NIIGATA	Mean Value (gal)	52	53	57	58	59
	C O V (%)	21.9	22.3	20.7	19.9	19.4
NAGOYA	Mean Value (gal)	260	260	262	263	263
	C O V (%)	5.4	5.4	3.6	3.9	3.9
KYOTO	Mean Value (gal)	87	90	91	93	94
	C O V (%)	10.6	11.9	12.2	13.1	13.5
OSAKA	Mean Value (gal)	85	94	94	99	100
	C O V (%)	28.9	24.7	27.7	28.3	28.2
HIROSHIMA	Mean Value (gal)	83	96	99	104	108
	C O V (%)	23.0	27.2	25.3	26.2	25.2
TAKAMATU	Mean Value (gal)	107	110	123	124	129
	C O V (%)	32.4	30.1	28.4	28.2	27.0
FUKUOKA	Mean Value (gal)	93	104	117	133	137
	C O V (%)	23.4	23.7	22.1	22.4	22.0

C O V : Coefficient of Variation

maximum sample data rounded off to one decimal and parameters are decided by using the method of least squares.

**(6) Evaluation for extremal distribution of maximum ground acceleration**

Ten cities in Japan where earthquake observatories are situated are chosen as the points for calculating the maximum ground acceleration. The following attenuation law<sup>17)</sup> suited for standard clay is proposed by the Public Works Research Institute of the Ministry of Construction and is adopted in this analysis.

$$Acc_{max.} = 18.4 * 10^{0.302M} * \Delta^{-0.8} \dots \dots \dots (6)$$

where  $Acc_{max}$  = maximum ground acceleration,  $M$  = magnitude and  $\Delta$  = epicentral distance. The extremal distribution of the maximum ground acceleration is estimated as follows.

a) It is assumed that a mesh ( $i, j$ ) is a hypo-center, and the epicentral distance from the center of the mesh to a city is calculated.

b) Magnitude  $M_{ij}$  is obtained from the attenuation law for which the epicentral distance and an acceleration  $Acc_{max.}$  are substituted.

$$M_{ij} = g(Acc_{max.}, \Delta_{ij}) \dots \dots \dots (7)$$

c) The value of the distribution function  $F_{a_{ij}}$  (a) at a maximum ground acceleration  $Acc_{max.}$  is evaluated by using the shape parameter, the modal value and the characteristic largest value of the

extremal distribution of the magnitude in the mesh ( $i, j$ ) and  $M_{ij}$  obtained in the preceding section b).

d) The previous operation is done for each mesh for maximum ground acceleration. Then using the following equation, the distribution function at city  $F_a$  (a) is obtained.

$$F_a(a) = \prod_{i=1}^n \prod_{j=1}^m F_{a_{ij}}(a) \dots \dots \dots (8)$$

e)  $F_a$  (a) is obtained by the preceding operation from b) to d) for some ( $Acc_{max.}$ ) accelerations, and the relation between  $F_a$  (a) and a is plotted on Gumbel probability paper.

Thus, the extremal distributions of the maximum ground acceleration at main cities are obtained. Fig.14 and 15 show the distribution for 50-year maximum of maximum ground acceleration at Sendai and Tokyo, respectively. Moreover, in order to examine the nonstationariness, the expected values and the coefficients of variation of the distributions for 50-, 40-, 30-, 20-, and 10-year maximums of maximum ground acceleration in 1988 are shown in Table 1. Furthermore, the expected values and the coefficients of variation of the distributions for the 50-year maximum of maximum ground acceleration at the different starting points (1968 and 1988) are shown in Table 2.

**Table 2** The expected values and the coefficients of variation of the extremal distributions of maximum ground acceleration in 1968 and 1988

Name of City	Statistics	1968	1988
SAPPORO	Mean Value (gal)	49	46
	C O V (%)	12.9	14.6
SENDAI	Mean Value (gal)	151	143
	C O V (%)	29.9	28.8
TOKYO	Mean Value (gal)	239	229
	C O V (%)	30.1	30.0
NIIGATA	Mean Value (gal)	58	59
	C O V (%)	18.0	19.4
NAGOYA	Mean Value (gal)	261	263
	C O V (%)	3.8	3.9
KYOTO	Mean Value (gal)	96	94
	C O V (%)	12.4	13.5
OSAKA	Mean Value (gal)	139	100
	C O V (%)	16.0	28.2
HIROSHIMA	Mean Value (gal)	117	108
	C O V (%)	20.3	25.2
TAKAMATU	Mean Value (gal)	136	129
	C O V (%)	21.9	27.0
FUKUOKA	Mean Value (gal)	144	137
	C O V (%)	17.6	22.0

C O V : Coefficient of Variation

#### 4. RESULTS AND CONSIDERATIONS

##### (1) Relative strain energy accumulation

Fig.5 to 7 show the relative strain energy accumulation in each cluster at present. It can be recognized that most meshes in each cluster are distributed near the boundary of the plate of the Pacific side in Kanto, Tohoku and Hokkaido, and many earthquakes occur in those places. Moreover, it can be assumed that a large earthquake is likely to occur in places in which the strain energy accumulation is high such as in cluster 3 at present.

##### (2) Extremal distribution of the magnitude in each mesh

The distributions for the 50-year maximum of magnitude in the meshes near Sendai are shown in Fig.10 to 13. Judging from theoretical curve of the type III extreme value distribution, those distributions accounting for the relative strain energy accumulation at present obviously fit the type III extreme value distribution. The probability of the occurrence of a large earthquake is greater as the strain energy accumulation at present increases. For example, comparing Fig.11 with Fig.12, which show the distribution for the 50-year maximum of magnitude in the meshes at cluster 2, the magnitude at a probability exceeding 0.2 is less than 7.5 in Fig.12 and 7.0 in Fig.11, respectively, because the strain energy accumulation at present in Fig.12 is higher than that in Fig.11.

Therefore, it is thought that the form of the

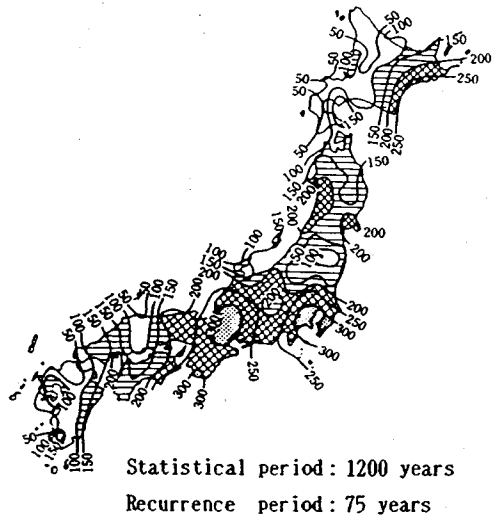


Fig.16 Seismic risk map by Gotou and Kameda

distribution of the 50-year maximum of magnitude remains unchanged, but that the magnitude at the probability of occurrence varies depending on the strain energy accumulation at present.

##### (3) Extremal distribution of maximum ground acceleration at main cities

The distributions for the 50-year maximum of maximum ground acceleration at main cities are shown in Fig.14 and 15. Those distributions fit the type III extreme value distribution as do the distributions for the 50-year maximum of magnitude. The expected values and the coefficients of variation of the distributions for 50-, 40-, 30-, 20- and 10-year maximums of maximum ground acceleration in 1988 are shown in Table 1. Those values reflect the strain energy accumulation at present in the mesh in which the cities are located. Comparing the expected values for  $n=50$  years in Table 1 with the seismic risk map of maximum ground acceleration by Gotou and Kameda<sup>18)</sup> in Fig.16, the expected values yielded by this analysis for Kyoto and Osaka are low extremely. It seems that extensive earthquake data were available for the Kyoto area in which population and culture have been concentrated, because the analysis by Gotou and Kameda used historical earthquake data based on estimations from ancient records.

##### (4) Examination of nonstationariness in maximum ground acceleration.

According to Table 1, the expected values of extremal distribution of maximum ground acceleration at Sapporo and Niigata are almost constant from  $n=10$  years to  $n=50$  years because the seismicities of these cities are not active. However, in other cities, there are large differences in the expected values between  $n=10$  years and  $n=50$



years ; in particular, the difference in Tokyo is 40 gal. Moreover, the expected values and the coefficients of variation of the distributions for the 50-year maximum of maximum ground acceleration at the different starting points (1968 and 1988) are shown in **Table 2**. According to **Table 2**, the difference of the expected values in Niigata and Nagoya are small, but about 10 gal in Tokyo and Sendai, and 40 gal in Osaka. So, it is recognized that the expected value of maximum ground acceleration varied due to the strain energy accumulation at that time. Therefore, it is necessary to consider the nonstationariness in earthquake occurrence when determining the earthquake load in design.

## 5. CONCLUSIONS

This analysis employed seismic risk analysis in which the focal regions which would have an influence on Japan were restricted. This zone was divided by meshes with  $0.5^\circ$  angles, and relative strain energy accumulation in each mesh was estimated by taking account of the nonstationariness in earthquake occurrence. Moreover, the distributions for the 50-year maximum of magnitude in each mesh were evaluated. Furthermore, the extremal distributions of maximum ground acceleration at the main cities were derived by means of the attenuation law. From this analysis, the following conclusions can be said.

(1) A procedure of seismic risk analysis taking account of the relative strain energy accumulation was proposed.

(2) The distributions for the 50-year maximum of magnitude in each mesh fitted the type III extreme value distribution very well.

(3) As the strain energy accumulation at present increases, the value of magnitude at a probability of occurrence becomes greater.

(4) The distributions for the 50-year maximum of maximum ground acceleration at main cities fitted the type III extreme value distribution as did magnitude.

(5) The expected value of maximum ground acceleration at a city reflected the strain energy accumulation at present in the mesh in which the city is located.

(6) This analysis is capable of forecasting the earthquake load suited to the service life of a structure. That is, it is possible to determine a more rational earthquake load in design by estimating the strain energy accumulation at the time when the structure will be constructed.

(7) This analysis is capable of evaluating the extremal distributions for maximum ground acceleration and those expected values in all parts of

Japan, and it seems that these statistics are useful for the criterion of aseismic design.

As above mentioned, this seismic risk analysis is capable of taking into account the nonstationariness in earthquake occurrence by estimating the strain energy accumulation in each mesh at present. So, with this analysis, it is possible to forecast earthquakes by adopting new earthquake data and to estimate the earthquake load suited to the service life of a structure. However, the data on large earthquakes with recurrence periods of 200 to 300 years are probably insufficient because the earthquake data of the past 100 years in Japan as measured by seismograph are used in this analysis. In this analysis, the seismicity gaps are not treated and the attenuation law is used to cope with standard clay. So, for obtaining more accurate findings, it is necessary that the attenuation law used is suited to each place and conditions of clay.

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### 震源域のひずみエネルギー蓄積状態を考慮した 地震危険度解析

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本研究では、過去100年程度の地震データから推定された震源域のひずみエネルギー蓄積状態を基に、将来発生するであろう地震の規模および最大加速度を地震発生の非正常性を考慮に入れ、統計確率論的に評価する手法を提案した。その結果、最大加速度の最大値分布は極値Ⅲ型漸近分布に適合すること、および同一地点であっても、その時点でのひずみエネルギー蓄積状態に応じて最大加速度の期待値が異なり、設計地震荷重を決定する際には、地震発生の非正常性を考慮に入れた解析が必要であること、などを指摘した。